Advanced Algebra II with Statistics Pre-Requisite Summer Packet

Solving Equations

1. If 4x - 8 = 26, what is the value of 2x - 8?

Solve the following equations:

2.
$$3(x-1) - x = 3 + 2(x-3)$$

3. $2x - \frac{5}{6} = \frac{3}{4}x$
4. $\frac{2}{5}a - \frac{1}{2} = -\frac{1}{2}a + 1$

Solve the following equations for x:

5.
$$m = \frac{x+n}{p}$$
 6. $\frac{cx+dx}{a} = g$

7. What value of a makes this equation have a solution of all real numbers? 2x - ax - 15 = a(2x - 3) - 13x

Linear Functions

8. What is the slope of the line passing through (-5,9) and (-5,6)?

9. The graph of Ax + 3y = -3 is a line that passes through the point (2,-5). What is the value of A?

10. Write an equation of a line that is perpendicular to the line 6x - 9y = 45.

11. Write an equation for the line in slope-intercept form that passes through the points (-3,-11) and (2,-1).

12. Use the table to write an equation of the line in all 3 forms:

x	у	Point-slope:
-10	-7	
0	-3	Slope Intercept:
5	-1	
20	5	Standard:

13. Determine the value of k so that the line goes through (k, 6) and (1, 2) and is parallel to the graph of 2x+y=3.

14. Graph y = -4x + 6 on the domain $x \le 0$. Then find the range of the function.



15. Find the 200th term of the arithmetic sequence 6, 1, -4, -9,

Functions

16. Describe the transformations from f(x) to h(x).

a.)
$$f(x) = x^{2}$$

 $h(x) = \frac{1}{3}(x-4)^{2}$
b.) $f(x) = |x|$
 $h(x) = -|x| + 4$

17. If
$$f(x) = 3x-1$$
 and $g(x) = 5x$, find:a.) $f(g(-4))$ b.) $g(f(1))$ c.) $g(f(x))$





19. Given the graph, answer the following questions:



Inequalities

Solve and write the solution in interval notation.

$$20.\frac{1}{3} + x + \frac{2}{9} \ge \frac{5}{6}$$
 . $21.4x + 8 \ge x + 6 \text{ or } 7x - 14 \ge 2x - 4$

22.
$$4y + 3 < y$$
 and $y - 3 < 2y - 15$
23. $4 \left| x + \frac{1}{3} \right| = 20$

$$24. \ -\frac{1}{3} |6x - 3| \ge -3$$

Systems of Equations

25. If x + y = 5 and x + 2y = 10, what is x - y?

26. Solve the system:
$$\frac{3}{4}x = y - 4$$

 $4y - 3x = 5$
 $\frac{4x + 5y = 44}{27}$
27. Solve the system: $3x - 2y = 10$

28.
$$ax + \frac{1}{4}y = 7$$
 For what values of *a* does the system have no solution? _____
 $\frac{1}{3}x + \frac{1}{6}y = 3$ For what values of *a* does the system have infinitely many solutions? _____

For what values of *a* does the system have exactly one solution?

Exponents and Exponential Functions

29. Simplify the following. No negative exponents should remain.

a.
$$(-2)^2(-2)^4$$
 b. $(-2)(-2)^7$ c. $[(-2)^4]^4$ d. $36^{\frac{3}{2}}$

e.
$$(-8)^{\frac{2}{3}}$$
 f. $(81x^6)^{\frac{3}{4}}$ g. $y \cdot y^{x-2} \cdot y^x$ h. $\left(\frac{1}{-4x^3}\right)\left(\frac{2}{-4x^3}\right)(-4x)^{-2}$

30. Solve for r: 81 $^{-\frac{3}{4}}$ = 27^r

31. If $x^2 \cdot x^2 \cdot x^2 = \frac{x^3 \cdot x^3}{r}$, then r =

32. Write an exponential function that represents the data in the table:

х	-2	-1	0	1	2
у	1/9	1/3	1	3	9

33. Write an exponential function that passes through the given points:

х	-2	-1	0	1	2
У	24	12	6	3	3/2

Factoring

Factor the following expressions completely.

34. $3x^2 - 75y^2$	35. 2a ³ + 16a ² + 30a	36. $12x^4 + 10x^3 - 12x^2$

$$37.1 - 16x^4 38.x^4 - 26x^2 + 25 39.6x^2 + 9x - 105$$

40. Solve for x: $0 = -27x^3 + 9x^2 + 6x$

41. Solve for k if the polynomial is a perfect square trinomial: $4x^2 - 20x + k$

Quadratics

42. What are the x-intercepts of $f(x) = -x^2 + 13x - 36$?

43. What is the vertex of the graph of $y = -2x^2 + 16x - 15$?

44. Solve the quadratic equation: $a^2 + 8a = 18$

45. Solve $\frac{2}{5}(x-4)^2 = 16$. Answer should be exact and in simplest radical form.

46. Solve by completing the square: $x^2 - 10x + 26 = 8$

47. Solve by using the quadratic formula: $2x^2 - 8x = 7$. Answer should be exact and in simplest radical form.

Radicals

48. Simplify
$$\sqrt{\frac{80 w^3}{9}}$$
 49. Simplify $\frac{7\sqrt{100}}{\sqrt{500}}$ 50. Simplify $4\sqrt{7}$ + $8\sqrt{63}$

51. Simplify $\sqrt{\frac{63x^4}{7xy}}$ 52. $(6 - \sqrt{11})(6 + \sqrt{11})$

53. Determine the length of the missing side:



Rational Expressions

Simplify. State any excluded values.

$$54. \frac{x^2 - x}{x^2 + x - 2} \qquad 55. \frac{9a^2 - 25}{2a - 2} \div \frac{6a - 10}{a^2 - 1} \qquad 56. \frac{9}{5x - 10} + \frac{4}{4x - 8}$$