Exercise Set 1.1: An Introduction to Functions

Find the domain of each of the following functions. Then express your answer in interval notation.

$$1. \quad f(x) = \frac{5}{x-3}$$

$$f(x) = \frac{x-6}{x+1}$$

3.
$$g(x) = \frac{x-4}{x^2-9}$$

4.
$$f(x) = \frac{3x+1}{x^2+4}$$

5.
$$f(x) = \frac{x^2 + 6x + 5}{x^2 - 11x + 28}$$

6.
$$g(x) = \frac{3x+15}{x^2+8x-20}$$

7.
$$f(x) = \frac{2}{\sqrt{x-4}}$$

$$8. \qquad f(x) = \sqrt{x-5}$$

$$g(x) = \sqrt{x+7}$$

10.
$$F(x) = \frac{\sqrt{3-2x}}{x+4}$$

$$11. \qquad G(x) = \frac{\sqrt{x-3}}{x-7}$$

12.
$$g(x) = \frac{-3}{\sqrt{x^2 - 4}}$$

13.
$$f(x) = |x^2 - 4|$$

Evaluate the following.

14. If
$$f(x) = 5x - 4$$
, find:

$$f(3), f(-\frac{1}{2}), f(a), f(a+3), f(a)+3, f(a)+f(3)$$

15. If
$$f(x) = \frac{2+x}{x-3}$$
, find:

$$f(-7), f(0), f(\frac{3}{5}), f(t), f(t^2-3)$$

If
$$g(x) = x^2 - 3x + 4$$
, find:
 $g(0), g(-\frac{1}{4}), g(x+5), g(\frac{1}{a}), g(3a), 3g(a)$

Transformations of Functions – Extra Practice

Write an equation for a function that has a graph with the given characteristics.

- 1. The shape of $y = x^2$ but is shifted left 3 units
- 2. The shape of $y = \sqrt{x}$ but upside down and shifted right 3 units and up 4 units.
- 3. The shape of y = |x| but stretched vertically by a factor of 2 and shifted right 3 units.
- 4. The shape of $y = x^2$ but upside-down and shifted right 8 units
- 5. The shape of y = |x| but stretched horizontally by a factor of 2 and shifted down 5 units
- 6. The shape of $y = x^3$ but reflected across the x-axis and shifted up 1 unit.
- 7. The shape of $y = \sqrt{x}$ but reflected across the y axis, shifted down 2, and left 4.
- 8. The shape of $y = x^2$ but compressed vertically by a factor of 2 and shifted up 6.