

Describe how the graph of  $g$  is obtained from the graph of  $f$ . (Do not sketch the graph.)

21.  $f(x) = \sqrt{x}$ ,  $g(x) = \sqrt{-x} - 2$  reflect over  $y$ , down 2
22.  $f(x) = x^3$ ,  $g(x) = -2(x+5)^3$  reflect over  $x$ , vertical stretch(2)  
left 5
23.  $f(x) = |x|$ ,  $g(x) = -5|x-2|+1$  reflect over  $x$ , vertical stretch(5)  
right 2, up 1
24.  $f(x) = x^2$ ,  $g(x) = \frac{1}{6}(x+3)^2 - 7$  vertical compression of  $\frac{1}{6}$ , left 3  
down 7
25.  $f(x) = \frac{1}{x}$ ,  $g(x) = \frac{3}{x+8} + 2$  left 8, up 2, vertical stretch by 3
26.  $f(x) = \sqrt[3]{x}$ ,  $g(x) = \sqrt[3]{-x} + 4$  reflect over  $y$ , up 4

Describe how the graphs of each of the following functions can be obtained from the graph of  $y = f(x)$ .

27.  $y = f(x) + 1$  up 1
28.  $y = f(x - 7)$  right 7
29.  $y = f(-x) + 3$  reflect over  $y$ , up 3
30.  $y = -f(x + 3) - 8$  left 3, down 8, reflect over  $x$  axis
31.  $y = -\frac{1}{4}f(x - 2) - 5$  reflect over  $x$ , vertical compression  $\frac{1}{4}$   
right 2, down 5
32.  $y = -5f(-x) + 1$  reflect over  $x$ , vertical stretch by 5, reflect  $y$
33.  $y = f(7 - x) + 2$  reflect over  $y$ , left 7, up 2 up 1
34.  $y = f(-x - 5) - 7$  reflect over  $y$ , right 5, down 7

**Matching.** The left-hand column contains equations that represent transformations of  $f(x) = x^2$ . Match the equations on the left with the description on the right of how to obtain the graph of  $g$  from the graph of  $f$ .

**D** 7.  $g(x) = (x - 4)^2$

A. Reflect in the  $x$ -axis.

**J** 8.  $g(x) = x^2 - 4$

B. Shift left 4 units, then reflect in the  $y$ -axis.

**F** 9.  $g(x) = x^2 + 4$

C. Reflect in the  $x$ -axis, then shift downward 4 units.

**I** 10.  $g(x) = (x + 4)^2$

D. Shift right 4 units.

**A** 11.  $g(x) = -x^2$

E. Shift right 3 units, then reflect in the  $x$ -axis, then shift upward 4 units.

**G** 12.  $g(x) = (-x)^2$

F. Shift upward 4 units.

**K** 13.  $g(x) = 4x^2$

G. Reflect in the  $y$ -axis.

**L** 14.  $g(x) = \frac{1}{4}x^2$

H. Shift left 4 units, then shift upward 3 units.

**C** 15.  $g(x) = -x^2 - 4$

I. Shift left 4 units.

**H** 16.  $g(x) = (x + 4)^2 + 3$

J. Shift downward 4 units.

**E** 17.  $g(x) = -(x - 3)^2 + 4$

K. Stretch vertically by a factor of 4.

**B** 18.  $g(x) = (-x + 4)^2$

L. ~~Shrink~~ Shrink vertically by a factor of  $\frac{1}{4}$ .

**Compress**