

Simplifying Trig Expressions

$$\cos(\theta) \tan(\theta)$$

$$\cos \theta \cdot \frac{\sin \theta}{\cos \theta} = \boxed{\sin \theta}$$

$$\sin(\theta) \cot(\theta)$$

$$\sin \theta \cdot \frac{\cos \theta}{\sin \theta} = \boxed{\cos \theta}$$

$$\csc^2(x) \tan^2(x)$$

$$\frac{1}{\sin^2 \theta} \cdot \frac{\sin^2 \theta}{\cos^2 \theta} = \frac{1}{\cos^2 \theta} = \boxed{\sec^2 \theta}$$

$$\sin(x) \sec(x) \cot^2(x)$$

$$\sin(x) \cdot \frac{1}{\cos(x)} \cdot \frac{\cos^2(x)}{\sin^2(x)} = \frac{\cos(x)}{\sin(x)}$$

$$= \boxed{\cot(x)}$$

$$\cot(x) \csc(x) \tan^2(x)$$

$$\frac{\cos(x)}{\sin(x)} \cdot \frac{1}{\sin(x)} \cdot \frac{\sin^2(x)}{\cos^2(x)} = \frac{1}{\cos(x)}$$

$$= \boxed{\sec(x)}$$

$$\frac{1 - \sin^2(x)}{\cos^2(x) - 1} = \frac{\cos^2(x)}{-\sin^2(x)} = \boxed{-\cot^2(x)}$$

Name Key

$$\cos(\theta) [\sec(\theta) - \cos(\theta)]$$

$$\cos \theta \sec \theta - \cos^2 \theta$$

$$\left(\frac{\cos \theta}{1} \cdot \frac{1}{\cos \theta} \right) - \cos^2 \theta$$

$$1 - \cos^2 \theta = \boxed{\sin^2 \theta}$$

$$\sin(\theta) [\csc(\theta) - \sin(\theta)]$$

$$\sin \theta \csc \theta - \sin^2 \theta$$

$$\left(\frac{\sin \theta}{1} \cdot \frac{1}{\sin \theta} \right) - \sin^2 \theta$$

$$1 - \sin^2 \theta$$

$$\boxed{\cos^2 \theta}$$

$$\sin(x) [\cot(x) + \tan(x)]$$

$$\sin(x) \cot(x) + \sin(x) \tan(x)$$

$$\left[\frac{\sin(x) \cdot \cos(x)}{1 \cdot \sin(x)} \right] + \left[\frac{\sin(x) \cdot \sin(x)}{1 \cdot \cos(x)} \right]$$

$$\frac{\sin(x) \cos(x)}{\sin(x)} + \frac{\sin^2(x)}{\cos(x)} = \frac{\sin(x) \cos^2(x) + \sin^3(x)}{\sin(x) \cos(x)}$$

$$\frac{\sin(x) [\cos^2(x) + \sin^2(x)]}{\sin(x) \cos(x)} = \frac{1}{\cos(x)} = \boxed{\sec(x)}$$

$$\cos(x) [\tan(x) + \cot(x)]$$

$$\frac{\cos(x) \cdot \sin(x)}{1 \cdot \cos(x)} + \frac{\cos(x) \cdot \cos(x)}{1 \cdot \sin(x)}$$

$$\frac{\cos(x) \sin(x)}{\cos(x)} + \frac{\cos^2(x)}{\sin(x)} = \frac{\cos(x) \sin^2(x) + \cos^3(x)}{\sin(x) \cos(x)}$$

$$\frac{\cos(x) [\sin^2(x) + \cos^2(x)]}{\sin(x) \cos(x)} = \frac{1}{\sin(x)}$$

$$= \boxed{\csc(x)}$$

$$\begin{aligned}
 \star \cos x \cdot (\csc x + \tan x) &= \\
 &= \cos x \left(\frac{1}{\sin x} + \frac{\sin x}{\cos x} \right) = \\
 &= \cos(x) \left(\frac{\cos(x)}{\sin(x)\cos(x)} + \frac{\sin^2 x}{\sin(x)\cos(x)} \right) \\
 &= \frac{\cos^2(x) + \cos^2(x)\sin^2(x)}{\sin(x)\cos(x)} \\
 &= \frac{\cos^2(x)(1 + \sin^2(x))}{\sin(x)\cos(x)} \\
 &= \frac{\cos^3(x)\cos^2(x)}{\sin(x)\cos(x)} \\
 &= \boxed{\cot(x)\cos^2(x)}
 \end{aligned}$$

$$\begin{aligned}
 \star \cot(\theta) \sec^2(\theta) - \cot(\theta) &= \\
 &= \cot(\theta) (\sec^2 \theta - 1) \\
 &= \cot(\theta) (\tan^2 \theta) \\
 &= \frac{\cos \theta}{\sin \theta} \cdot \frac{\sin^2 \theta}{\cos^2 \theta} = \frac{\sin \theta}{\cos \theta} \\
 &= \boxed{\tan \theta}
 \end{aligned}$$

$$\star \sin^2 t \cos^2 t (1 + \tan^2 t)$$

$$= \sin^2 t \cos^2 t \sec^2 t$$

$$= \sin^2 t \cos^2 t \frac{1}{\cos^2 t}$$

$$= \boxed{\sin^2 t}$$

$$\tan^2(x) + 1 = \sec^2(x)$$

$$\sin^2(x) + \cos^2(x) = 1$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

Simplifying Trig Expressions (more advanced)

Foil

$$[\sec(x) - \tan(x)][\sec(x) + \tan(x)]$$

$$\sec^2(x) - \tan^2(x)$$

$$\boxed{1}$$

Pyth
Identity

Foil

$$[\csc(x) - \cot(x)][\csc(x) + \cot(x)]$$

$$\csc^2(x) - \cot^2(x)$$

$$\boxed{1}$$

Pyth
Identity

See extra paper

$$\frac{\cot(x) + \tan(x)}{\csc^2(x)}$$

$$\boxed{\tan(x)}$$

$$\frac{\sec^2(x)}{\tan(x) + \cot(x)}$$

$$\boxed{\tan(x)}$$

$$[1 - \cos(x)][\csc(x) + \cot(x)]$$

$$\csc(x) + \cot(x) - \cos(x)\csc(x) - \cos(x)\cot(x)$$

$$\frac{1}{\sin(x)} + \frac{\cos(x)}{\sin(x)} - \left(\frac{\cos(x)}{1} \cdot \frac{1}{\sin(x)}\right) - \left(\frac{\cos(x)}{1} \cdot \frac{\cos(x)}{\sin(x)}\right)$$

$$\frac{1 + \cos(x) - \cos(x) - \cos^2(x)}{\sin(x)} = \frac{1 - \cos^2(x)}{\sin(x)} = \frac{\sin^2(x)}{\sin(x)} = \boxed{\sin(x)}$$

$$[\csc(x) - 1][\sec(x) + \tan(x)]$$

$$\csc(x)\sec(x) + \csc(x)\tan(x) - \sec(x) - \tan(x)$$

$$\frac{1}{\sin(x)\cos(x)} + \left[\frac{1}{\sin(x)} \cdot \frac{\sin(x)}{\cos(x)}\right] - \frac{1}{\cos(x)} - \frac{\sin(x)}{\cos(x)}$$

$$\left[\frac{1 + \sin(x)}{\sin(x)\cos(x)}\right] + \left[\frac{-1 - \sin(x)}{\cos(x)}\right] \cdot \begin{matrix} (\sin(x)) \\ (\sin(x)) \end{matrix}$$

$$= \frac{1 + \sin(x) - \sin(x) - \sin^2(x)}{\sin(x)\cos(x)}$$

$$= \frac{1 - \sin^2(x)}{\sin(x)\cos(x)} = \frac{\cos^2(x)}{\sin(x)\cos(x)} = \frac{\cos(x)}{\sin(x)} = \boxed{\cot(x)}$$

$$\frac{\cos(x)}{1 - \sin(x)} - \frac{\cos(x)}{1 + \sin(x)}$$

$$\boxed{2 \tan(x)}$$

$$\frac{\cot(\theta)}{\csc(\theta) + 1} + \frac{\cot(\theta)}{\csc(\theta) - 1}$$

$$\boxed{2 \sec \theta}$$

$$\frac{\cot(x) + \tan(x)}{\csc^2(x)} = \frac{\left[\frac{\cos(x)}{\sin(x)} + \frac{\sin(x)}{\cos(x)} \right]}{\frac{(\cos^2(x) + \sin^2(x))}{\sin(x)\cos(x)}} = \frac{1}{\sin^2(x)} \cdot \frac{\sin^2(x)}{1} = \frac{\sin(x)}{\cos(x)} = \boxed{\tan(x)}$$

$$\frac{\sec^2(x)}{\tan(x) + \cot(x)} = \frac{\left[\frac{1}{\cos^2(x)} \right]}{\frac{\frac{\sin x}{\cos x} + \frac{\cos x}{\sin x}}{\sin(x)\cos(x)}} = \frac{\left[\frac{1}{\cos^2(x)} \right]}{\frac{1}{\sin(x)\cos(x)}} = \frac{1}{\cos^2(x)} \cdot \frac{\sin(x)\cos(x)}{1} = \frac{\sin(x)}{\cos(x)} = \boxed{\tan(x)}$$

$$\frac{\cos(x)}{-\sin(x)} - \frac{\cos(x)}{1+\sin(x)} = \frac{\cos(x)[1+\sin(x)]}{1-\sin^2(x)} - \frac{\cos(x)[1-\sin(x)]}{1-\sin^2(x)} \quad \left(\begin{array}{l} \text{Don't forget...} \\ \text{Distribute the} \\ \text{negative!!} \end{array} \right)$$

$$= \frac{(\cos(x) + \sin(x)\cos(x)) - (\cos(x) - \sin(x)\cos(x))}{1-\sin^2(x)} = \frac{2\sin(x)\cos(x)}{\cos^2(x)} = \frac{2\sin(x)}{\cos(x)} = \boxed{2\tan(x)}$$

$$\frac{\cot\theta}{\csc\theta + 1} + \frac{\cot\theta}{\csc\theta - 1} = \frac{\cot\theta[\csc\theta - 1]}{\csc^2\theta - 1} + \frac{\cot\theta[\csc\theta + 1]}{\csc^2\theta - 1}$$

$$= \frac{\cot\theta \csc\theta - \cot\theta + \cot\theta \csc\theta + \cot\theta}{\csc^2\theta - 1} \xrightarrow{\text{Pyth Identity}} \frac{2\cot\theta \csc\theta}{\cot^2\theta} = \frac{2\csc\theta}{\cot\theta} = \frac{\left(\frac{2}{\sin\theta}\right)}{\left(\frac{\cos\theta}{\sin\theta}\right)} = \frac{2}{\cos\theta} = \boxed{2\sec\theta}$$