

Multiplying and Dividing Rational Expressions

Simplify each expression.

$$1) \frac{n^2 - 11n + 24}{n^2 + 2n - 48} \cdot \frac{n^2 + 14n + 48}{n + 6}$$

$$\boxed{\frac{(n-8)(n-3)}{n-6}} \cdot \frac{(n-3)(n-8) \cdot (n+6)(n+8)}{(n+8)(n-6) \cdot (n+6)}$$

$$2) \frac{4x+8}{x^2+4x+4} \cdot \frac{7x^2+14x}{4x+36} \cdot \frac{4(x+2)}{(x+2)(x+2)} \cdot \frac{7x(x+2)}{4(x+9)}$$

$$\boxed{\frac{7x}{x+9}}$$

$$3) \frac{3(3x^2+4x+1)}{9x^2+12x+3} \cdot \frac{20x-12}{30x^2+30x}$$

$$\boxed{\frac{2}{5x}} \cdot \frac{3(3x+1)(x+1) \cdot 4(5x-3)}{30x(x+1) \cdot (5x-3)(3x+1)}$$

$$4) \frac{25x^2-30x}{2x^2+28x+90} \cdot \frac{2x^2+24x+70}{5x-6}$$

$$\boxed{\frac{5x(x+7)}{x+9}} \cdot \frac{5x(5x-6) \cdot (2x+10)(x+7)}{2(x+5)(x+9) \cdot (5x-6)}$$

$$5) \frac{3p+7}{9p^2+27p+14} \div \frac{1}{3p^2+32p+20}$$

$$\boxed{p+10} \cdot \frac{(3p+7)}{(3p+2)(3p+7)} \cdot \frac{(3p+2)(p+10)}{1}$$

$$6) \frac{1}{n-10} \div \frac{2n+8}{2n^2+4n-16}$$

$$\frac{1}{n-10} \cdot \frac{2(n+4)(n-2)}{2(n+4)}$$

$$\boxed{\frac{n-2}{n-10}}$$

$$7) \frac{5}{\frac{4}{x} - \frac{x}{5}}$$

$$\frac{5}{\frac{20-x^2}{5x}} = \frac{5}{\frac{5}{x}} = \frac{5x}{20-x^2}$$

$$\boxed{\frac{25x}{20-x^2}}$$

$$8) \frac{a-4}{\frac{4}{9} + \frac{1}{3}}$$

$$\frac{a-4}{\frac{4}{9} + \frac{3}{9}} = \frac{a-4}{\frac{7}{9}} = \frac{a-4}{1} \cdot \frac{9}{7}$$

$$\boxed{\frac{9a-36}{7}}$$

$$9) \frac{\frac{9}{x^2}}{\frac{x}{16} + \frac{3}{4}} = \frac{\frac{9}{x^2}}{\frac{x}{16} + \frac{12}{16}} = \frac{\frac{9}{x^2}}{\frac{x+12}{16}}$$

$$\boxed{\frac{144}{x^3+12x^2}}$$

$$\frac{9}{x^2} \cdot \frac{16}{x+12}$$

** Distribute the minus **

$$10) \frac{\frac{x-1}{x+3} - \frac{1}{x}}{x-1}$$

$$\frac{\frac{x^2-x}{x(x+3)} + \frac{-x-3}{x(x+3)}}{\frac{x-1}{1}}$$

$$\boxed{\frac{x^2-2x-3}{x^3+2x^2-3x}}$$

$$\frac{x^2-2x-3}{x(x+3)} \cdot \frac{1}{x-1}$$