

Pre-Calculus Final Exam Extra Practice

Given the table below:

$x$	$\frac{\pi}{2}$	$\frac{3\pi}{4}$	$\pi$	$\frac{5\pi}{4}$	$\frac{3\pi}{2}$
$y$	0.5	0	-0.5	0	0.5

Which function fits the data?

- A  $y = 0.5 \cos(2x - \pi)$
- B  $y = 0.5 \cos(x - \pi)$
- C  $y = 0.5 \cos\left(2x + \frac{\pi}{2}\right)$
- D  $y = \cos\left(2x + \frac{\pi}{2}\right)$

In a geometric sequence,  $a_1 = 12$  and  $r = \sqrt{2}$ . What is the **approximate** sum of the first 20 terms of the sequence?

- A 339.4
- B 8,688.9
- C 29,624.9
- D 29,636.9

A bathroom floor has tiles arranged in 9 circles. The innermost circle contains 9 tiles. Each successive circle contains 9 more tiles than the previous circle. How many total tiles are on the bathroom floor?

- A 81
- B 396
- C 405
- D 729

Pre-Calculus Final Exam Extra Practice

A Ferris wheel has a diameter of 80 feet. Riders enter the Ferris wheel at its lowest point, 5 feet above the ground, at time  $t = 0$  seconds. One complete rotation takes 65 seconds.



Which function models a rider's vertical height,  $h(t)$ , at  $t$  seconds?

- A  $h(t) = -80 \cos\left(\frac{2\pi}{65}t\right) + 5$
- B  $h(t) = -40 \cos\left(\frac{2\pi}{65}t\right) + 45$
- C  $h(t) = -45 \cos\left(\frac{65}{2\pi}t\right) + 40$
- D  $h(t) = -5 \cos\left(\frac{65}{2\pi}t\right) + 80$

How does the graph of  $g(x) = 0.5\cos(2x)$  differ from the graph of its parent function,  $f(x) = \cos(x)$ , over the interval  $-\pi \leq x \leq \pi$ ?

- A The amplitude is smaller, and the period is shorter.
- B The amplitude is smaller, and the period is longer.
- C The amplitude is larger, and the period is shorter.
- D The amplitude is larger, and the period is longer.

Pre-Calculus Final Exam Extra Practice

Two sides of a triangle measure 14 ft and 17 ft, respectively. The included angle is  $72^\circ$ . **Approximately** how long is the third side of the triangle?

- A 18.4 ft
- B 20.3 ft
- C 25.1 ft
- D 30.7 ft

What is the solution to the equation below?

$$\frac{\frac{3}{x} + 2}{\frac{x}{5} + 1} = \frac{15}{x}$$

- A  $^{-}12$
- B  $^{-}2$
- C 2
- D 12

Which is the solution set for  $x$  if  $2e^{2x} + 5e^x - 12 = 0$ ?

- A  $\left\{\ln\frac{3}{2}, \ln 4\right\}$
- B  $\left\{\ln\frac{3}{2}, \ln^{-}4\right\}$
- C  $\{\ln 4\}$
- D  $\left\{\ln\frac{3}{2}\right\}$

Pre-Calculus Final Exam Extra Practice

What value of  $h$  is needed to complete the square for the equation  $x^2 + 10x - 8 = (x - h)^2 - 33$ ?

- A  $-25$
- B  $-5$
- C  $5$
- D  $25$

Which expression is equivalent to  $\frac{\cos(\theta)}{1 - \sin(\theta)} - \tan(\theta)$ ?

- A  $\sec(\theta)$
- B  $\sin(\theta)$
- C  $\cos(\theta)$
- D  $\csc(\theta)$

William put the tip of his pencil on the outer edge of a graph of the unit circle at the point  $(0, -1)$ . He moved his pencil tip through an angle of  $\frac{4\pi}{3}$  radians in the counterclockwise direction along the edge of the circle. At what angle of the unit circle did William's pencil tip stop?

- A  $\frac{\pi}{3}$
- B  $\frac{5\pi}{6}$
- C  $\frac{7\pi}{6}$
- D  $\frac{5\pi}{3}$

Pre-Calculus Final Exam Extra Practice

Which is the inverse of  $f(x) = 1.5^x + 4$ ?

A  $f^{-1}(x) = \frac{x - 4}{1.5}$

B  $f^{-1}(x) = \frac{\log(x) - 4}{1.5}$

C  $f^{-1}(x) = \frac{\log(x - 4)}{\log(1.5)}$

D  $f^{-1}(x) = \frac{4 - \log(x)}{\log(1.5)}$

The recursive formula for a sequence is  $U_n = U_{n-1} + 12$ , where  $U_n$  is the  $n$ th term of the sequence and  $U_0 = 7$ . Which explicit formula can be used to determine the  $n$ th term of the sequence?

A  $7n + 19$

B  $7n + 12$

C  $7 + 19n$

D  $7 + 12n$

The volume of a rectangular prism is represented by the expression  $(x^3 - 2x^2 - 20x - 24)$ . If the length is  $(x - 6)$  and the height and width are equal, what is the width of the prism?

A  $x + 2$

B  $x - 2$

C  $x + 4$

D  $x - 4$

Pre-Calculus Final Exam Extra Practice

Which is an equation of a parabola that has a directrix of  $y = -5$  and a focus at  $(2, -1)$ ?

A  $y = \frac{1}{2}(x + 2)^2 + 2$

B  $y = \frac{1}{8}(x + 2)^2 + 3$

C  $y = \frac{1}{8}(x - 2)^2 - 3$

D  $y = \frac{1}{2}(x - 2)^2 - 2$

Given the function:

$$g(x) = \frac{(x - 2)(3x + 2)}{(x + 4)(x - 2)(x - 6)}$$

- What are the equations of the asymptotes of the function?
- Determine if there are any points of discontinuity. Explain why or why not.
- Describe the end behavior as  $x$  approaches  $-\infty$  and as  $x$  approaches  $+\infty$ .

The graph of  $f(x) = x^2$  will be translated 5 units up and 2 units to the right. Which function describes the graph produced by the translation?

A  $g(x) = x^2 - 4x + 9$

B  $g(x) = x^2 + 4x - 1$

C  $g(x) = x^2 - 10x + 27$

D  $g(x) = x^2 + 10x + 23$