

For each graph below, name the shape and the axis it is symmetric (positive x-axis, negative y-axis, etc).

$$r = 5 + 2 \sin \theta \quad \frac{\text{dimple}}{\text{limacon}} \quad \frac{\text{positive } y\text{-axis}}$$

$$r = 2 + 3 \cos \theta \quad \frac{\text{limacon}}{\text{w/inner loop}} \quad \frac{\text{positive } x\text{-axis}}$$

$$r = 2 - 2 \cos \theta \quad \frac{\text{cardioid}}{\quad} \quad \frac{\text{negative } x\text{-axis}}$$

For each rose curve, tell the number of petals and length of each petal.

$$r = 3 \sin 4\theta \quad \frac{8 \text{ petals}}{\quad} \quad \frac{3 \text{ units long}}{\quad}$$

$$r = 4 \sin 5\theta \quad \frac{5 \text{ petals}}{\quad} \quad \frac{4 \text{ units long}}{\quad}$$

Polar Graphs: Cardioid, Limacon with an Inner Loop, Dimpled Limacon, Rose, Circle, Ellipse

1. $r = 2\cos(5\theta)$

This graph is a Rose curve
It has 5 petals that are 2 units long

2. $r = 3 - 2\cos\theta$

This graph is a dimpled Limacon
symmetric about the neg. x-axis

3. $r = 4 + 4\sin\theta$

This graph is a cardioid
symmetric about the pos. y-axis

4. $r = 2 - 3\sin\theta$

This graph is a limacon w/inner loop
symmetric about the neg. y-axis

5. $r = 3\cos(2\theta)$

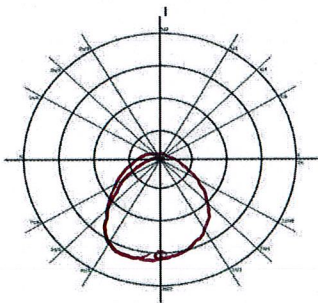
This graph is a Rose
It has 4 petals that are 3 units long

6. $r = 3$

This graph is a Circle
Centered at origin

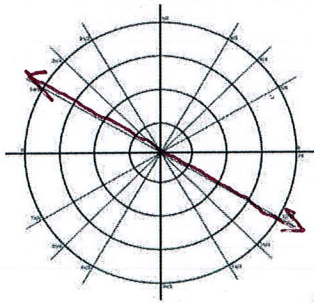
7. $r = -3\sin\theta$

This graph is a circle



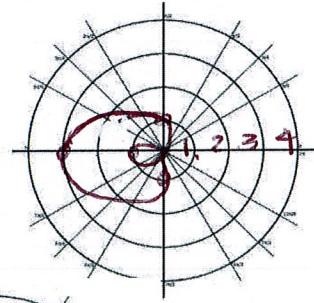
8. $\theta = \frac{11\pi}{6}$

This graph is a line



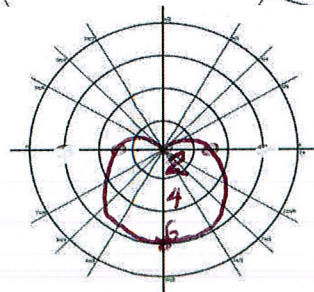
9. $r = 1 - 2\cos\theta$

This graph is a limacon w/inner loop



10. $r = 3 - 3\sin\theta$

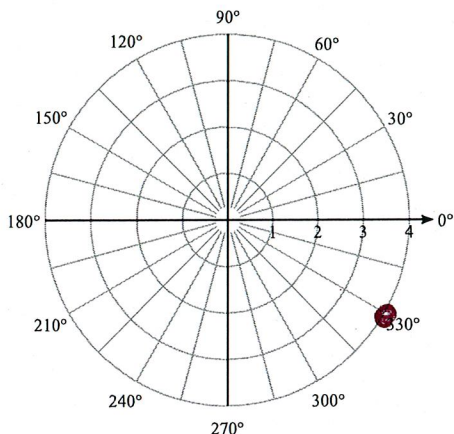
This graph is a cardioid



Extra Practice

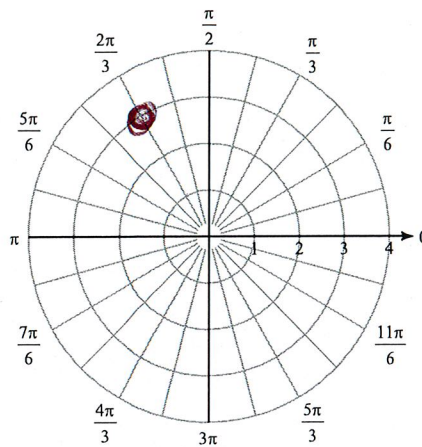
Plot the point with the given polar coordinates. State the three other pairs of polar coordinates for each point.

1) $(4, 330^\circ)$



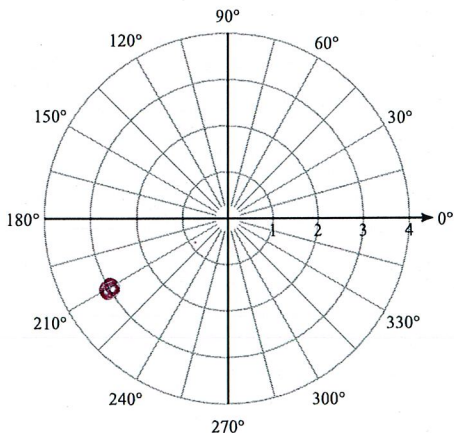
$(4, -30^\circ)$
 $(-4, 150^\circ)$
 $(-4, -210^\circ)$

2) $(3, -\frac{4\pi}{3})$



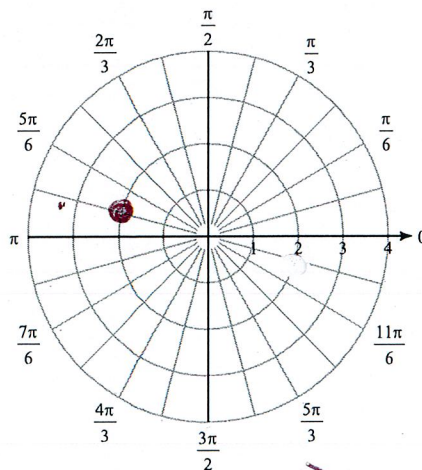
$(3, \frac{2\pi}{3})$
 $(-3, \frac{5\pi}{3})$
 $(-3, -\frac{\pi}{3})$

3) $(-3, 30^\circ)$



$(3, 210^\circ)$
 $(3, -150^\circ)$
 $(-3, -330^\circ)$

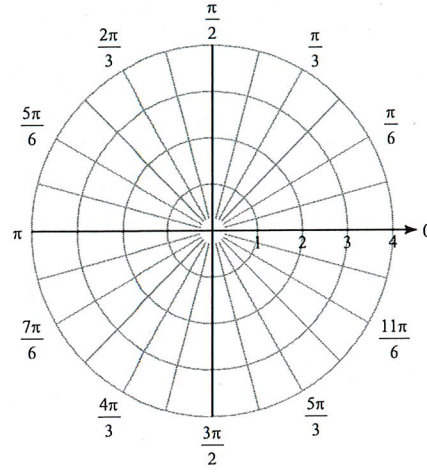
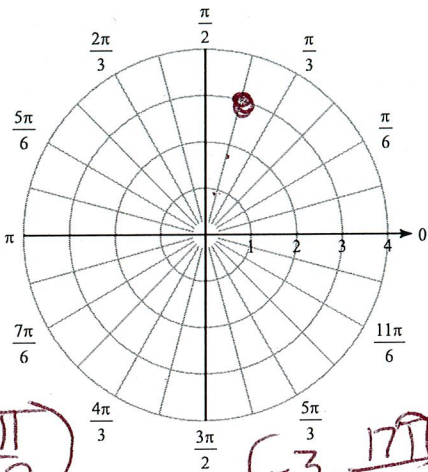
4) $(2, \frac{11\pi}{12})$



$(-2, -\frac{\pi}{12})$ $(2, -\frac{13\pi}{12})$
 $(-2, \frac{23\pi}{12})$

$$5) \left(3, -\frac{19\pi}{12} \right)$$

$$6) \left(-1, \frac{11\pi}{12} \right)$$



$$\begin{aligned} & \left(3, \frac{5\pi}{12} \right) \\ & \left(-3, -\frac{7\pi}{12} \right) \end{aligned}$$

Convert each pair of polar coordinates to rectangular coordinates.

$$7) \left(-2, \frac{11\pi}{6} \right) = (-\sqrt{3}, 1)$$

$$8) \left(1, \frac{3\pi}{4} \right) = \left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} \right)$$

$$9) \left(-1, \frac{3\pi}{2} \right) = (0, 1)$$

$$10) \left(-2, \frac{3\pi}{4} \right) = (\sqrt{2}, -\sqrt{2})$$

Convert each pair of rectangular coordinates to polar coordinates where $r > 0$ and $0 \leq \theta < 2\pi$.

$$11) \left(-\frac{1}{2}, \frac{\sqrt{3}}{2} \right) = \left(1, \frac{2\pi}{3} \right)$$

$$12) (-\sqrt{2}, -\sqrt{2})$$

$$= \left(2, \frac{5\pi}{4} \right)$$

positive
both
only

$$13) \left(-\frac{3\sqrt{3}}{2}, -\frac{3}{2} \right) = \left(3, \frac{7\pi}{6} \right)$$

$$14) (0, -1) = \left(1, \frac{3\pi}{2} \right)$$

Convert each equation from rectangular to polar form.

$$15) (x-2)^2 + (y-1)^2 = 5$$

$$r = 4\cos\theta + 2\sin\theta$$

$$16) x^2 + (y-1)^2 = 1$$

$$r = 2\sin\theta$$

$$17) (x+2)^2 + (y-1)^2 = 5$$

$$r = -4\cos\theta + 2\sin\theta$$

$$18) (x+3)^2 + y^2 = 9$$

$$r = -6\cos\theta$$