

## Domain and Range Notes

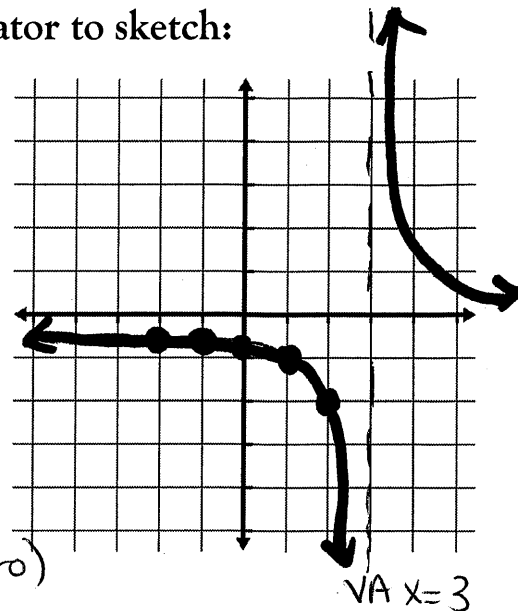
**Domain:** the set of all input values that yield a REAL number output value

- Domain describes the x values that give a real number answer for y

Fill in the table of values below then use your calculator to sketch:

$$y = \frac{4}{2x-6}$$

| x  | y                        |
|----|--------------------------|
| -2 | $4/-10 = -2/5$           |
| -1 | $4/-8 = -1/2$            |
| 0  | $4/-6 = -2/3$            |
| 1  | $4/-4 = -1$              |
| 2  | $4/-2 = -2$              |
| 3  | $4/0 = \text{undefined}$ |

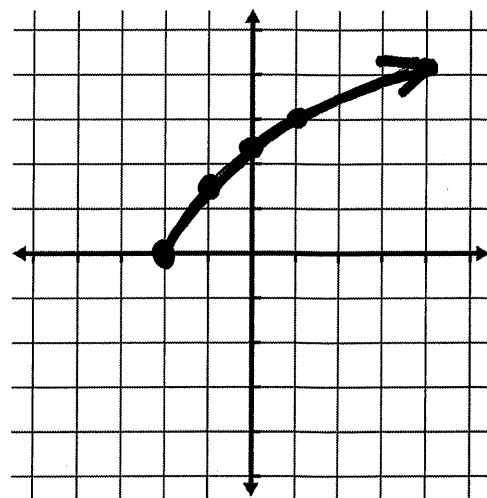


In a fraction, the denominator cannot equal 0 (zero)

Domain of  $y = \frac{4}{2x-6}$  would be  $2x-6 \neq 0$   
 $x \neq 3$   $(-\infty, 3) \cup (3, \infty)$

$$y = \sqrt{3x+6}$$

| x  | y                    |
|----|----------------------|
| -4 | $\sqrt{-6}$ not real |
| -3 | $\sqrt{-3}$ not real |
| -2 | $\sqrt{0} = 0$       |
| -1 | $\sqrt{3}$           |
| 0  | $\sqrt{6}$           |
| 1  | $\sqrt{9} = 3$       |



Under an even radical (square root), the radicand must be greater than or equal to zero

Domain of  $y = \sqrt{3x+6}$  would be

$$3x+6 \geq 0 \quad x \geq -2 \quad [-2, \infty)$$

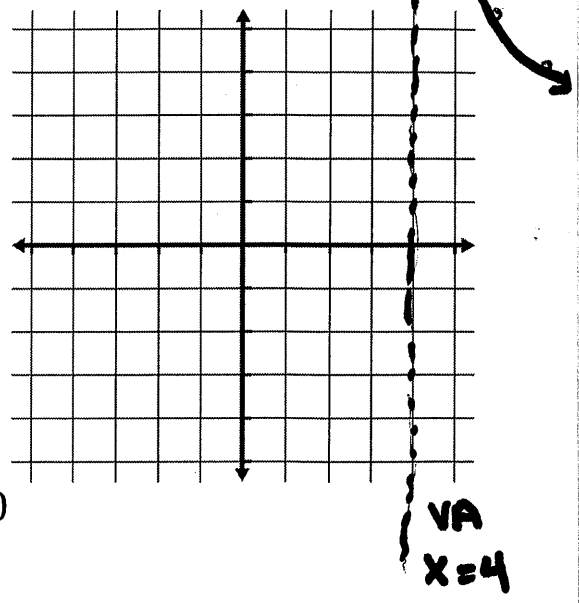
$$\geq 0$$

Domain and Range Notes

Fill in the table of values below then use your calculator to sketch:

$$y = \frac{8}{\sqrt{x-4}}$$

| x | y                         |
|---|---------------------------|
| 2 | $8/\sqrt{-2}$ not real    |
| 3 | $8/\sqrt{-1}$ not real    |
| 4 | $8/0$ undefined           |
| 5 | $8/\sqrt{1} = 8$          |
| 6 | $8/\sqrt{2} \approx 5.65$ |
| 7 | $8/\sqrt{3} \approx 4.62$ |



For this function, there is a fraction, so  $x - 4 \neq 0$

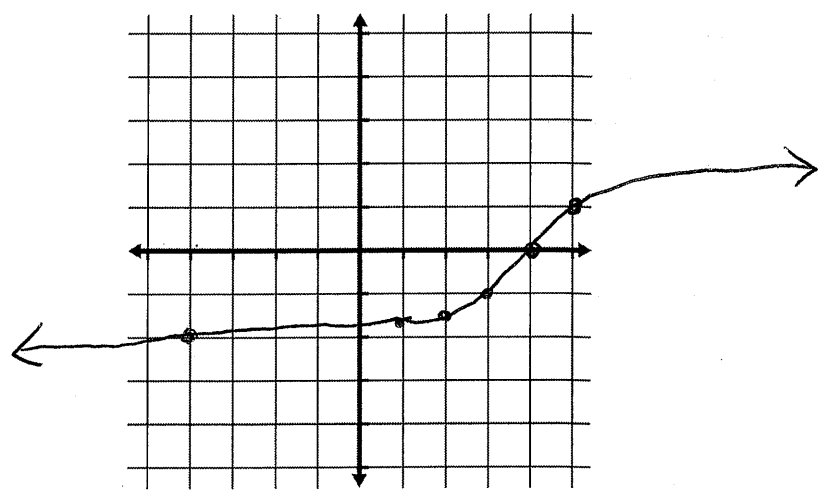
But, there is also a radical,  $x - 4 \geq 0$

If we put these ideas together, then  $x - 4 > 0$

Domain of  $y = \frac{8}{\sqrt{x-4}}$  would be  $x - 4 > 0$  so  $x > 4$   $(4, \infty)$

What about  $y = \sqrt[3]{x-4}$

| x | y                   |
|---|---------------------|
| 3 | $\sqrt[3]{-1} = -1$ |
| 4 | $\sqrt[3]{0} = 0$   |
| 5 | $\sqrt[3]{1} = 1$   |



Domain of  $y = \sqrt[3]{x-4}$

would be: All Real Numbers!

$\mathbb{R} \quad (-\infty, \infty)$