

Key

Logarithmic Functions HW

Write the logarithmic equation in exponential form

1. $\log_4 64 = 3$

$$4^3 = 64$$

2. $\log_7 \frac{1}{49} = -2$

$$7^{-2} = \frac{1}{49}$$

3. $\log_{32} 4 = \frac{2}{5}$

$$32^{\frac{2}{5}} = 4$$

Write the exponential equation in logarithmic form

4. $5^3 = 125$

$$\log_5 (125) = 3$$

5. $6^{-2} = \frac{1}{36}$

$$\log_6 (\frac{1}{36}) = -2$$

6. $81^{\frac{1}{4}} = 3$

$$\log_{81} (3) = \frac{1}{4}$$

Use the definition of the logarithmic function to find x.

7. $\log_2 x = 5$

$$x = 2^5 = [32]$$

8. $\log_2 16 = x$

$$2^x = 16 \quad [x=4]$$

9. $\log_{10} x = 2$

$$x = 10^2 = [100]$$

Use the properties of the logarithmic function to solve for x

10. $\log_4(3x - 2) = \log_4(x + 4)$

$$3x - 2 = x + 4$$

$$\begin{aligned} 2x &= 6 \\ x &= 3 \end{aligned}$$

11. $\log_5 1 = x$

$$\begin{aligned} 5^x &= 1 \\ x &= 0 \end{aligned}$$

12. $\log_3 3 = x$

$$\begin{aligned} 3^x &= 3 \\ x &= 1 \end{aligned}$$

13. $\log_5 5^2 = x$

$$\begin{aligned} 5^x &= 5^2 \\ x &= 2 \end{aligned}$$

Evaluate the expression

14. $\log_4 64$

$$4^x = 64$$

$$[x=3]$$

15. $\log_3 \frac{1}{27}$

$$3^x = \frac{1}{27}$$

$$[x=-3]$$

16. $\log_{16} 4$

$$16^x = 4$$

$$[x=\frac{1}{2}]$$

17. $\ln(\sqrt[5]{e^3})$

$$\begin{aligned} e^x &= \sqrt[5]{e^3} \\ x &= \frac{3}{5} \end{aligned}$$

18. $\log(\sqrt[3]{100})$

$$\begin{aligned} 10^x &= \sqrt[3]{100} \\ x &= \frac{2}{3} \end{aligned}$$

19. $\log_5 \left(\frac{1}{25}\right)$

$$\begin{aligned} 5^x &= \frac{1}{25} \\ x &= -2 \end{aligned}$$