

White 18-19  
White 20-23

# Electricity

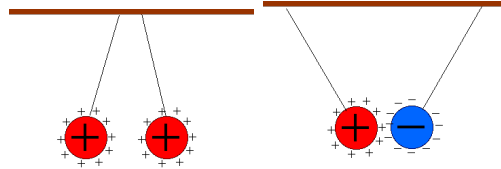
Ch 20-23 *Green*



### Charge

5 C  
5 μC 5 nC

- Positive or Negative charge
- Caused by an excess or absence of electrons. Unit is Coulomb (C)
- Like charges repel, opposites attract
- Proportional to the net force
- Electric fields: effect on other charges around it, strength depends on size of charge



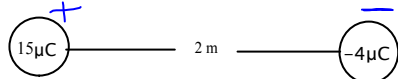
Mass: Electron  $9.11 \times 10^{-31}$  kg Proton & Neutron  $1.67 \times 10^{-27}$  kg  
 Charge: Electron  $= -1.6 \times 10^{-19}$  C Proton  $1.6 \times 10^{-19}$  C

How many electrons are in 1 Coulomb?  $K = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$

### Coulomb's Law Electric Force = $k(q_1q_2/r^2)$

$k = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$        $F_E = \frac{kq_1q_2}{d^2}$        $F = \frac{k|q_1||q_2|}{d^2}$

$k = \frac{1}{4\pi\epsilon_0} = 9 \times 10^9$



What is the Force between the two charges?

$$F = \frac{9 \times (15 \times 10^{-6}) \times (-4 \times 10^{-6})}{2^2}$$

$F = -.14 \text{ N}$

**Superposition:** use geometry to figure out the charge

1. Solve for the charge in between each one first
2. Use  $F_x \cos$   $F_y \sin$  for the one that is at an angle
3. Use Pythagorean theorem after that to find final charge

$A = 3 \text{ nC}$        $B = 6 \text{ nC}$       Find  $F$  on  $A$

$C = 9 \text{ nC}$

$F_{AC} = \frac{kq_A q_C}{d^2}$

$F_{AC} = \frac{9 \times (3 \times 10^{-9}) \times (9 \times 10^{-9})}{4^2}$

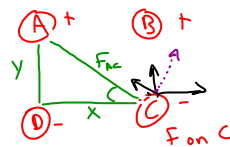
$F_{AC} = 1.52 \times 10^{-8} \text{ N}$

$F_{AB} = \frac{9 \times (3 \times 10^{-9}) \times (6 \times 10^{-9})}{3^2}$

$F_{AB} = 1.8 \times 10^{-8} \text{ N}$

Resultant force  $F$  with components  $1.8 \times 10^{-8}$  and  $1.52 \times 10^{-8}$

$F = 2.42 \times 10^{-8} \text{ N}$   
 at  $49.8^\circ$  w of n

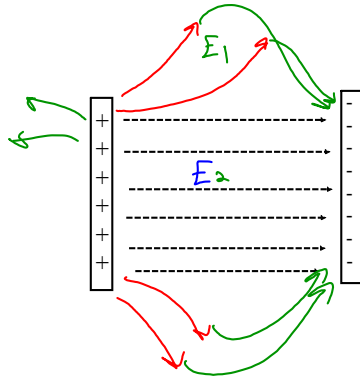
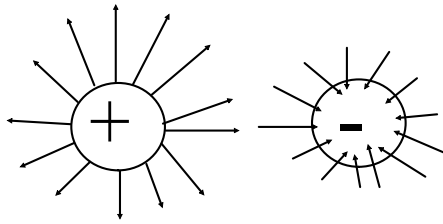


$$F_x = F_{DC} + F_{ACx}$$

$$F_y = F_{BC} + F_{ACy}$$

- Electric Field strength  $E = F/q_1$  The charge that the field is around
- $$E = \frac{Kq}{r^2} \quad E = \frac{F}{q} \quad \text{unit} = \text{N/C}$$

Electric field lines go out of the positive charge and into the negative charge



$$E = .15 \text{ N/C}$$

$$q = 3.5 \text{ nC}$$

$$F = ?$$

$$r = ?$$

$$E = F/q$$

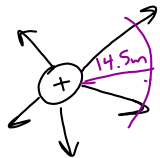
$$.15 = F / 3.5 \times 10^{-9}$$

$$F = 5.25 \times 10^{-10} \text{ N}$$

$$E = \frac{Kq}{r^2}$$

$$.15 = \frac{9 \times 10^9 (3.5 \times 10^{-9})}{r^2}$$

$$r = 14.5 \text{ m}$$



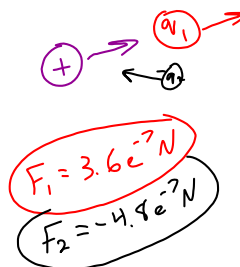
$$E = 2 \text{ N/C}$$

$$q_1 = 18 \times 10^{-9} \text{ C}$$

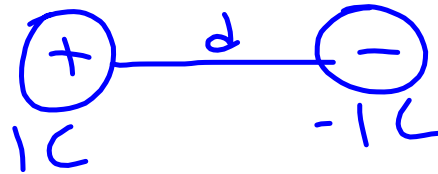
$$q_2 = -24 \times 10^{-9} \text{ C}$$

$$F_1 = ?$$

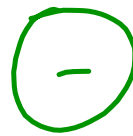
$$F_2 = ?$$



# Electric Dipole



<http://hyperphysics.phy-astr.gsu.edu/hbase/electric/dipole.html#c1>



Equilibrium- set the charges equal to one another and find the distance the new charge has to be placed inbetween them

$$F_{2,3} = kq_2q_3/p_{2,3}^2 = F_{3,1} = kq_3q_1/(d-l_{3,1})^2$$

$$q_1/d^2 = q_2/(L-d)^2$$

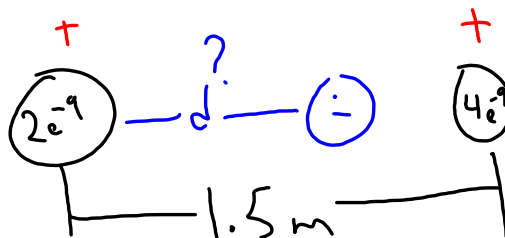
[ = total length  
A + C

Equilibrium

$$\frac{q_1}{d^2} = \frac{q_2}{(L-d)^2}$$

$$q_1 = 2e^{-9} C$$

$$q_2 = 4e^{-9} C$$



$$\frac{q_1}{d^2} = \frac{q_2}{(L-d)^2}$$

$$q_1 = 15e^{-6} C$$

$$q_2 = 6e^{-4} C$$

$$q_3 = (-)$$

$$\sum F = 0$$

$$L = 2m$$

$$d = ?$$

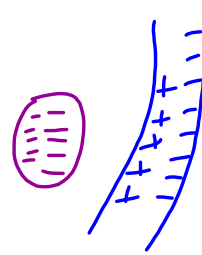


$$\frac{q_1}{d^2} = \frac{q_2}{(L-d)^2}$$

You will get 2 answers, you must determine which one makes sense for the setup.

## Static Charge

- How charge is transferred between objects
- By contact, friction, induction
- Always conserved in a system
- Friction: balloon and hair, feet on a rug
  - Some Atoms lose electrons easier than others
- Contact: charge moves through an object
- Induction: transfer with out contact because of repulsion



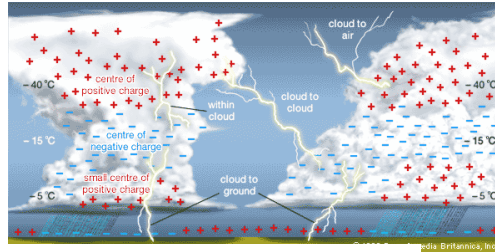
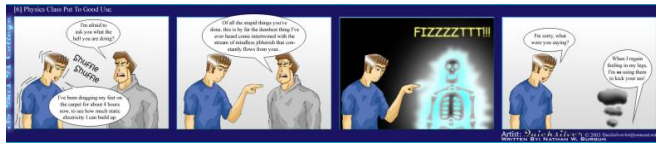
edison

electric man



# Static Discharge

- A pathway suddenly forms for charge to move
- Lightning bolt, a spark, a bolt

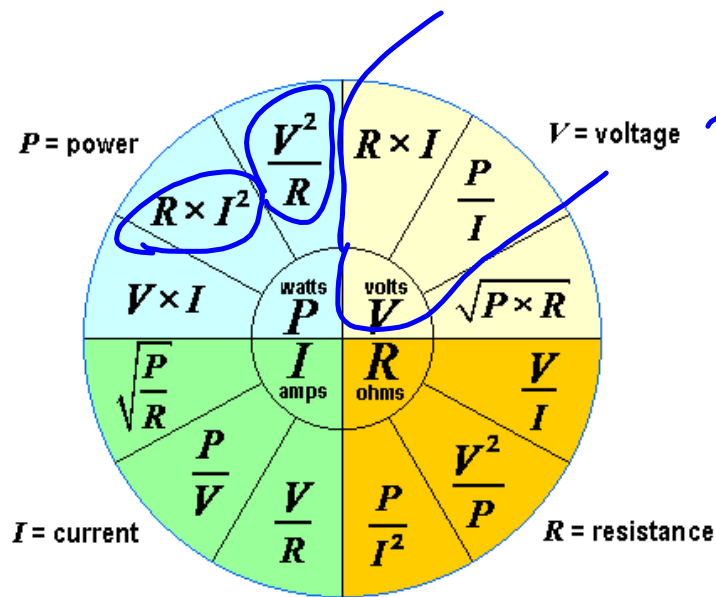


# Ohm's Law

21-22

$$V = IR$$

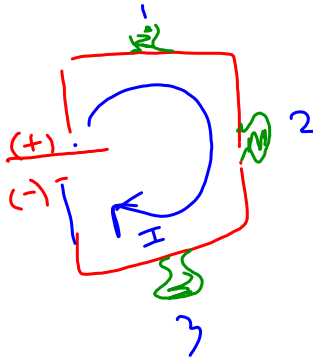
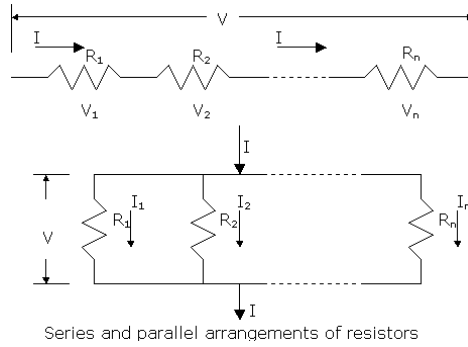
$$P = IV$$





Current (A) ~~symbol (I)~~  
 Symbol (I)

- Continuous flow of electron, unit is ampere (A)
- Direct Current (DC) flows in one direction
- Alternating Current (AC) flow regularly reverses direction
- $I = \frac{q}{\text{Time}}$
- Electrons move but in a diagram we should it as positives moving



doorknob current

$q = 3 \text{ C}$   
 $T = 10 \text{ s}$   
 $I = ?$

$I = .3 \text{ A}$

## Amps can kill

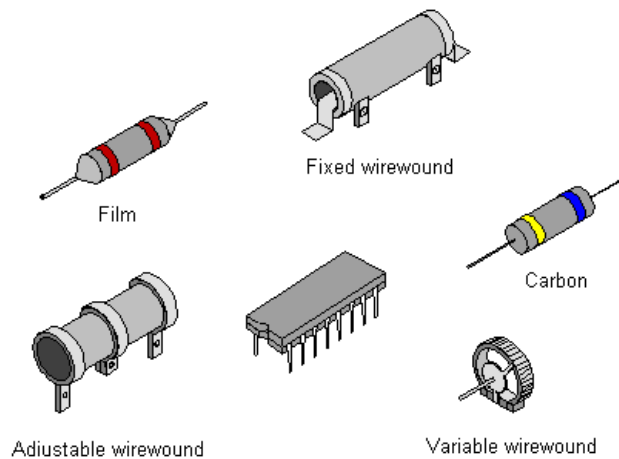
- .001 A tingles
- .005 A small shock
- .030 A painful, lose muscle control
- .100 A extreme pain, stop breathing
- 1.00 A nerve damage, heart stop, death
- 10.0 A severe burns, death is certain

# Resistance ( $\Omega$ )

Symbol  $R$

- Electrons have collisions with other electrons and ions and release thermal energy
- \* • Resistance- opposition to flow of electrons, unit is Ohms ( $\Omega$ )
  - Thickness, length, temperature affect resistance
- \* • Superconductor- near zero resistance

From Computer Desktop Encyclopedia  
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$$R = \rho \frac{L}{A}$$

Resistance measured in Ohms

$$R = \rho L / A$$

$\rho$  = resistivity of material

Green

chart on pg 721

Voltage (V)  $\Rightarrow \sum \mathcal{E} - \sum \mathcal{F}$

- Potential difference- difference in electrical potential energy between 2 places in an electric field, unit is voltage (V)
- Sources- batteries, solar cells, generators
- Battery: converts chemical energy into electric energy



$U_E = qV = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$

$U_E \sim k \frac{q_1 q_2}{r}$

EPE = qV

$E = Pt$  Energy = Power x time

Energy unit is kilowatt hour!  $U = k \frac{q_1 q_2}{r}$

hours 1kwh = 3,600,000

$U_E = PT$

Potential difference on a point charge

$V = kq/r$   $V = \frac{1}{4\pi\epsilon_0} k \left( \frac{q}{r} \right)$   $V = k \frac{q}{r}$

combining Electric field and Potential  $V = k \left( \frac{q_1}{r_1} + \frac{q_2}{r_2} \right)$

$E = -\nabla V$

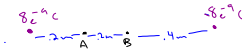
Gauss' Law  $E = q / \epsilon_0 A$

$q = 4 \times 10^{-9} C$   $V = \frac{kq}{r}$

$r = 1.2 m$

$V = ?$   $V = \frac{9 \times 10^9 (4 \times 10^{-9})}{1.2}$

$V = 3000 V$



$V_A = ?$   $V_B = ?$

$V_A = 9 \times 10^9 \left( \frac{2 \times 10^{-9}}{2} + \frac{6 \times 10^{-9}}{4} \right)$

$V_A = 72,000 V$

$V_B = 9 \times 10^9 \left( \frac{2 \times 10^{-9}}{2} + \frac{2 \times 10^{-9}}{2} \right)$

$V_B = 54,000 V$

$V_C = 9 \times 10^9 \left( \frac{6 \times 10^{-9}}{2} + \frac{2 \times 10^{-9}}{2} \right)$

$V_C = 198,000 V$

$U_T = U_A + U_B + U_C$

$U_T = 288,000 J$

$U_A = 5 \times 10^4 (72,000)$

$U_A = 360 J$

$U_B = 6 \times 10^4 (54,000)$

$U_B = 324 J$

$U_C = 2 \times 10^4 (198,000)$

$U_C = 396 J$

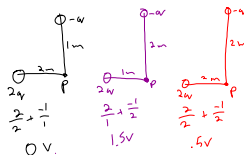
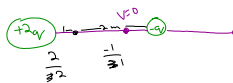
$U = U_A + U_B + U_C$

$V_{AC} = k \frac{q_A q_C}{r}$

$U_{AC} = 9 \times 10^4 V$

$V_{AB} = k \frac{q_A q_B}{r}$

$U_{AB} = 45 V$





$V_A = 108V$
$V_B = 36V$

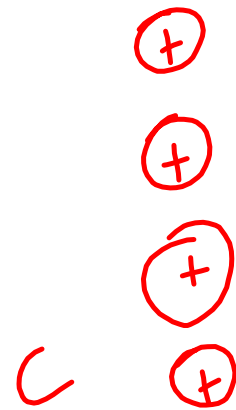
$$V_A =$$

$$V_B =$$

A charge's electric potential energy at any point is equal to the amount of work done in moving it there from its rest position.



B



$$q_1 = 15 \text{ nC}$$

$$V_A = 300 \text{ V}$$

$$V_B = -200 \text{ V}$$

$$U_E = ?$$

$$\Delta V = ?$$

$$r = .01 \text{ m}$$

$$V = ?$$

$$q = 1 \text{ nC}$$

Parallel plate capacitors- store charge. Have the same magnitude of opposite charge on two conductors with a separation between them.

$C = q/V$

$C = \frac{q}{V}$

unit F (f)  
Farad

$C = \epsilon_0 A/d$   
Parallel Plates

$C = \frac{K \epsilon_0 A}{d}$

$\epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{Nm^2}$   
 $A \rightarrow area$

dielectric constant for insulator  $d \rightarrow$  between plates

$U_c = 1/2 QV = 1/2 CV^2$

$E_c = q/0A$



- $K_{vac} \Rightarrow 1$
- $K_{air} \Rightarrow 1.00054 \approx 1$
- $K_{Teflon} \Rightarrow 2$

$C = 1.3 \mu F$   
 $V = 1.5 V$   
 $q = ?$

$C = 1 \mu F$   
 $d = .07 mm = .00007 m$   
 $A = ?$   
 $V = 1.5 V$   
 $q = ?$



$C = 220 \mu F$   
 $V = 330 V$   
 $U_c = ?$   
 $T = 1 ms$   
 $P = ?$

$U_c = 1/2 CV$

$U = PT$



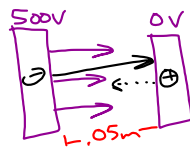
$d_1 = 5 \times 10^{-3} \text{ m}$   
 $d_2 = .15 \times 10^{-3} \text{ m}$   
 $A = 9.5 \times 10^{-5} \text{ m}^2$   
 $K = 3.5$   
 $\Delta C = ?$

$C_{\text{Final}} - C_{\text{Initial}}$   
 $C = \frac{K \epsilon_0 A}{D}$

$V_1 = 100 \text{ V}$   
 $V_2 = 30 \text{ V}$

$E = \frac{V_e}{d}$

$C = 150 \mu\text{F}$   
 $V = 2000 \text{ V}$   
 $d = .01 \text{ mm}$   
 $K = 300$   
 $A = ?$   
 $V_c = ?$



$e^- = 1.6 \times 10^{-19} \text{ C}$   
 $d = .05 \text{ m}$   
 $V_f = ?$   
 $V_i = 0 \text{ m/s}$   
 $U_c = ?$

Ch 20: 5,9,15,20,23,24,27,29

problems 4,9,10,16,18,24,26,30,48,49

Ch 21: 2,7,18,23,24,25,28,30

problems

2,6,12,16,22,27,28,31,36,37,39,42,59,65

## Ohm's Law



\* •  $V=IR$

$$V=IR$$

- Voltage = Current x Resistance

## Power

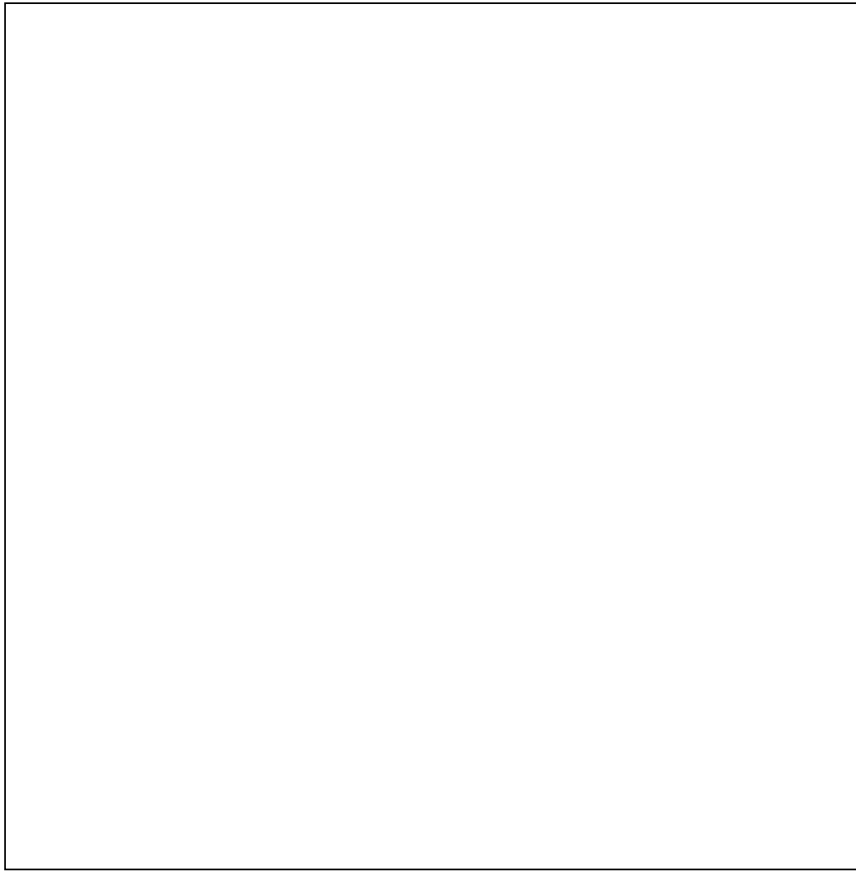
$$P=IV$$

$$P=I^2R$$

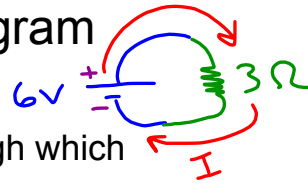
$$P=\frac{V^2}{R}$$

- \* •  $P=IV$  Power = Current x Voltage
- Power unit is watts
- $P=V^2/R$     $P=I^2R$     $P=IV$

$$EE = Pt$$

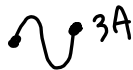


# Circuit Diagram

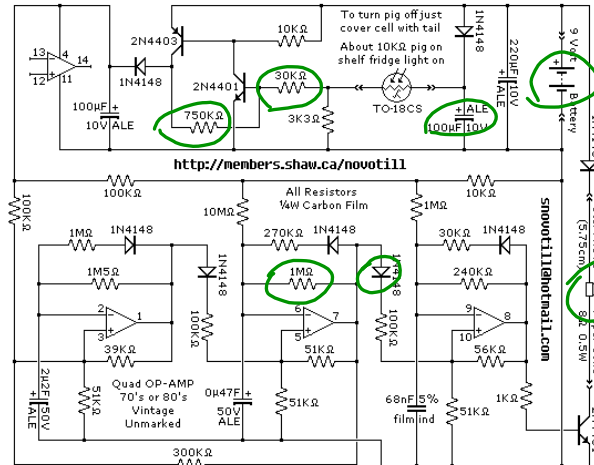


• Circuit- a complete path through which charge can flow

- Use symbols
- Battery
- Resistor
- Current direction
- Voltage
- Capacitor
- Fuse



REFRIGERATOR PIG - Dinks when fridge door is opened and light hits the photocell at the pig's tail. Sound isn't particularly authentic



<http://www.kpsec.freeuk.com/symbol.htm>

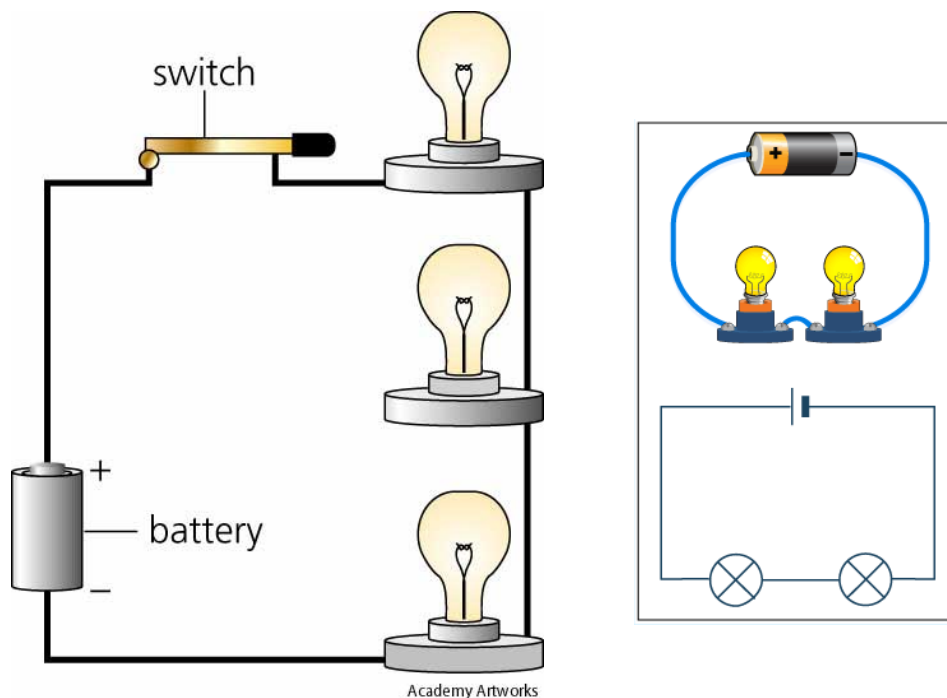


[http://talkingelectronics.com/CctSymbols/Circuit\\_Symbols.html](http://talkingelectronics.com/CctSymbols/Circuit_Symbols.html)

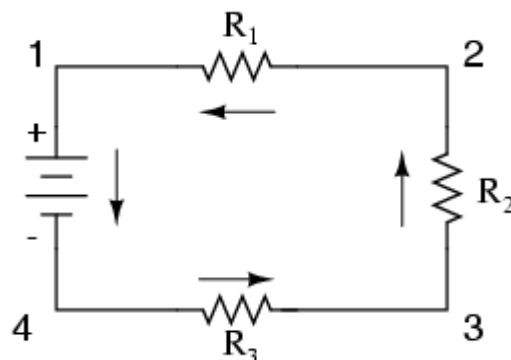


## 2 Types of Circuit

- Series: only one path to follow, a circle
- If chain is broken everything stops moving and working
- Adding bulbs to a series increases the resistance, so every bulb is less bright because it gets less current
  - To find  $V, I, R$  across a resistor you must first find  $R_{\text{Total}}, I_{\text{total}}, V_{\text{total}}$
- $R_{\text{total}} = R_1 + R_2 + R_3 + \dots$
- Current stays the same across all resistors
- Voltage Changes at each resistor

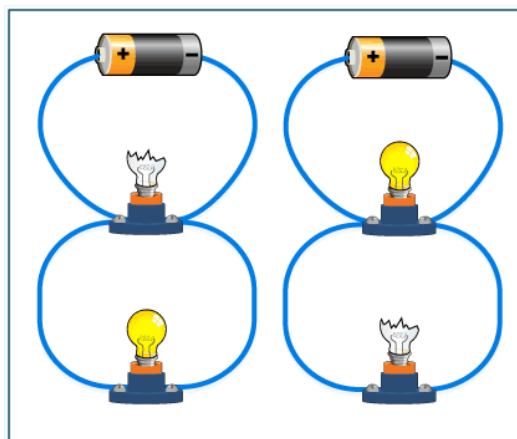
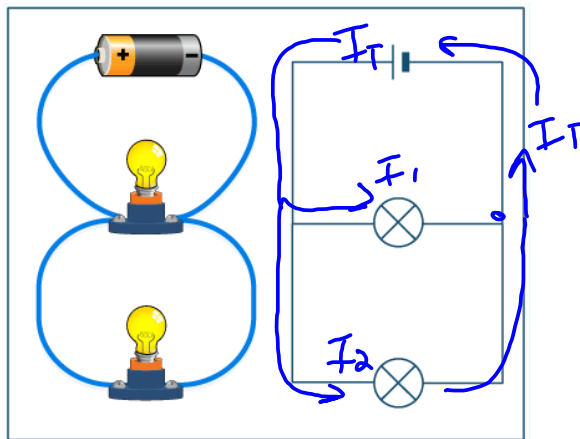


### Series

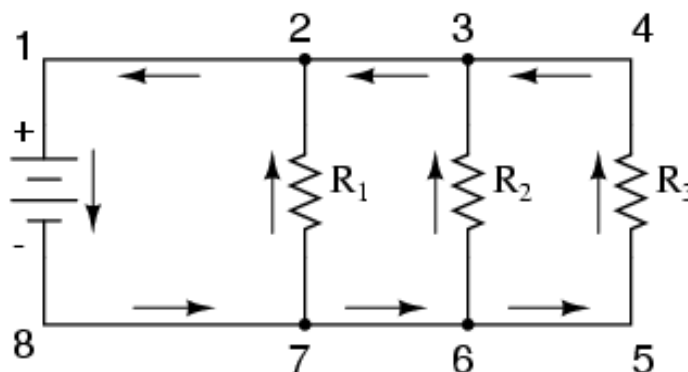


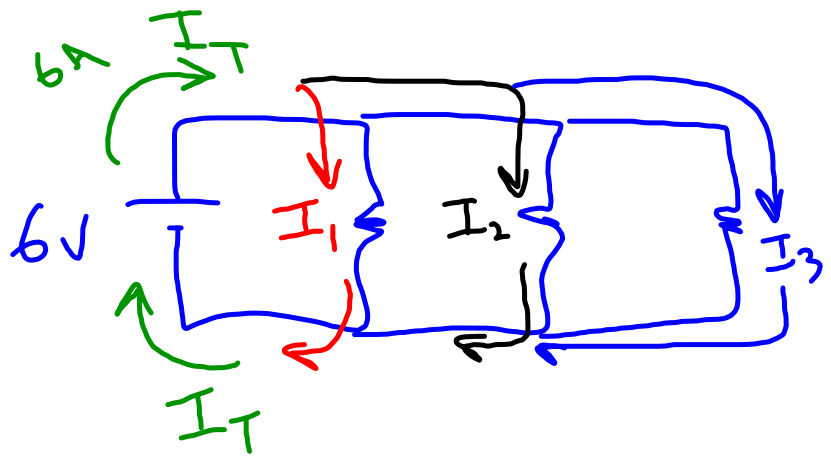
# Parallel Circuit

- 2 or more possible path for charge to follow
- If one chain is broke the current will continue to follow the other paths
- This is how homes are wired
- $R_{total} = 1/R_1 + 1/R_2 + 1/R_3 + \dots$
- Current changes across each resistor
- Add up to I Total
- Voltage same across each resistor



Parallel

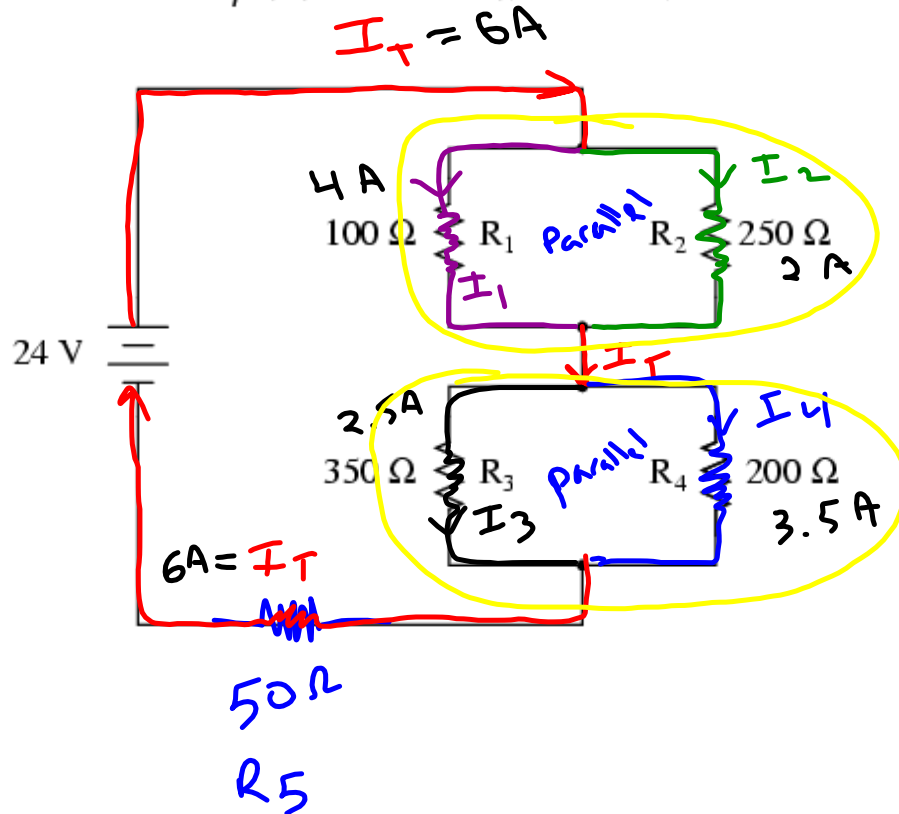


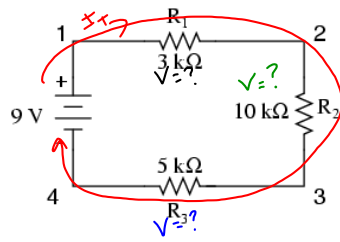




- Combination Circuit
- You can have combination of series and parallel circuits in one large circuit
- Reduce it down to make 1 simple circuit

*A series-parallel combination circuit*

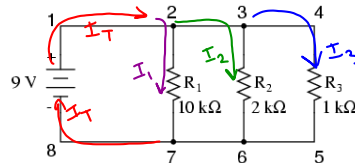




$V = I R$   
 $V_1 = .0005 (3000)$   
 $V_2 = .0005 (10,000)$   
 $V_3 = .0005 (5000)$

V	I	R	P
1.5V	.0005	3000 Ω	
5V	.0005	10,000 Ω	
2.5V	.0005	5,000 Ω	

$V_T = 9V$

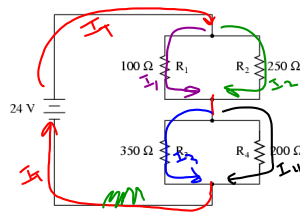


$V = I R$   
 $9 = I (10000)$   
 $V = I R$   
 $9 = I (2000)$   
 $9 = I_3 (1000)$

V	I	R	P
0V	.0009A	10,000 Ω	
9V	.0045A	2,000 Ω	
9V	.009A	1,000 Ω	

$V_T = 9V$      $I_T = A$

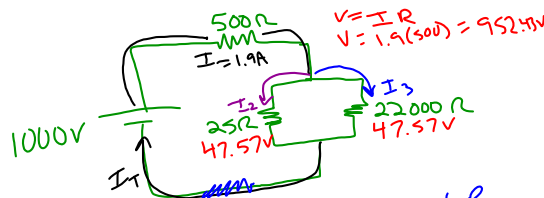
A series-parallel combination circuit



$I_1 + I_2 = I_T$   
 $I_2 = .121A$   
 $I_3 + I_4 = .121A$

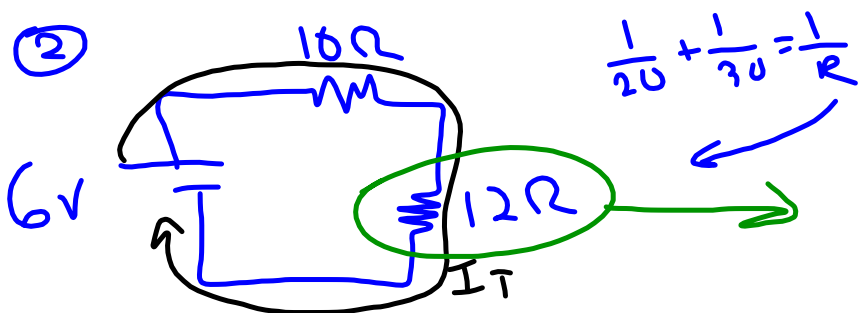
V	I	R	P
6.63	.0463	100 Ω	
8.63	.03452	250 Ω	
15.4	.044	350 Ω	
15.4	.077	200 Ω	

$V_T = 24V$



$V_T = V_1 + V_2$   
 $1000 = 952.43 + V_2$

V	I	R
952.43	1.9A	500Ω
47.57	1.89A	25Ω
47.57	.002A	22000Ω



$$\frac{1}{20} + \frac{1}{30} = \frac{1}{R}$$

$$V = IR$$

$$V = .27(12)$$

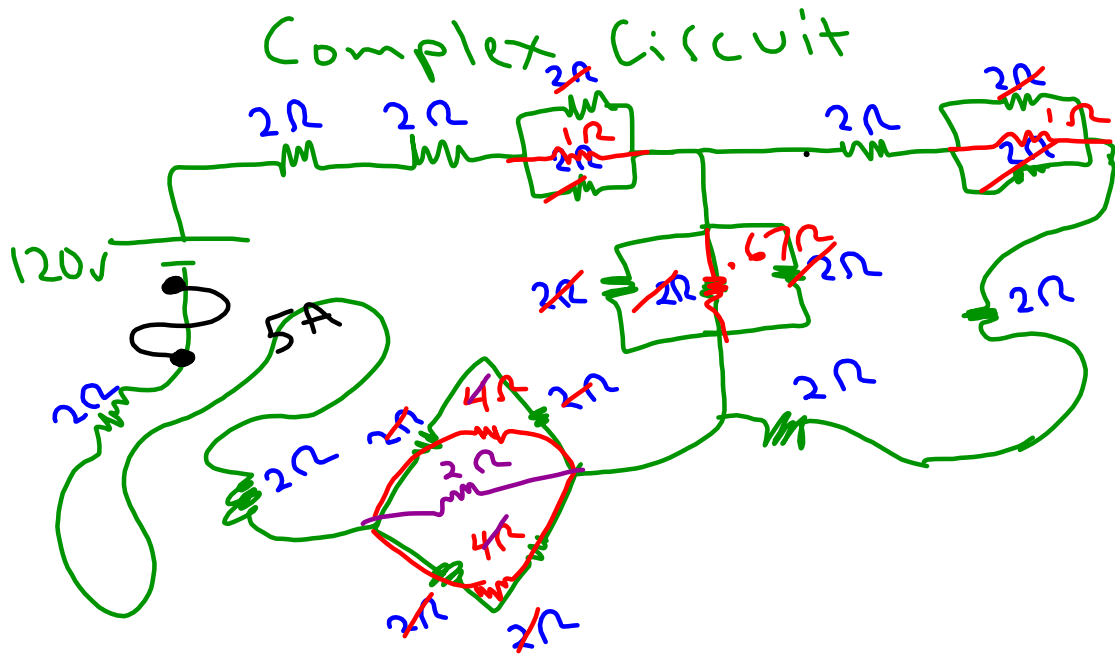
$$V = 3.25V$$



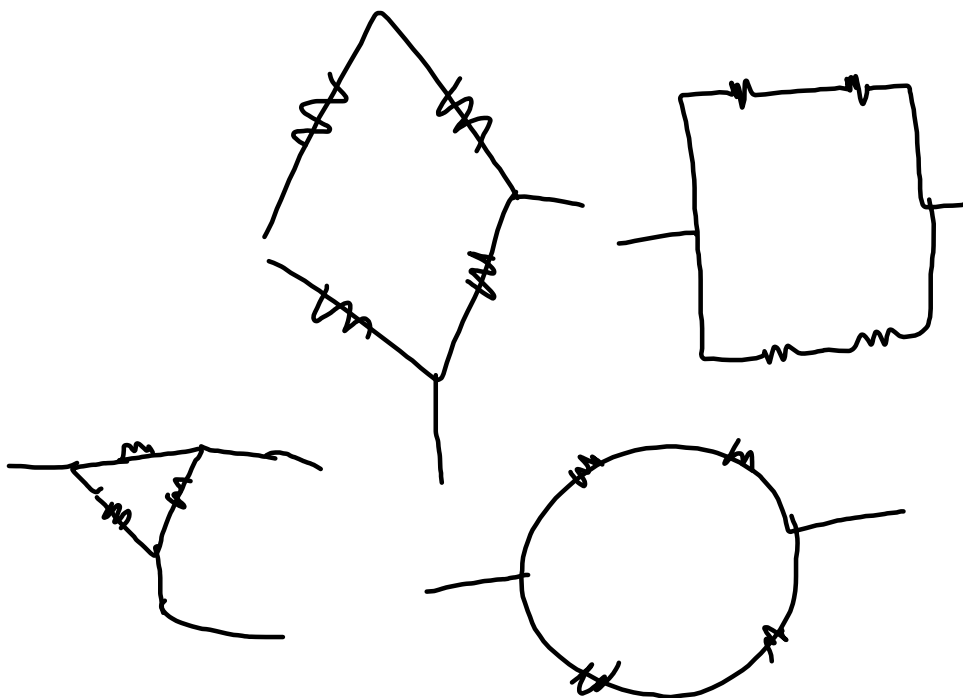
$$V = IR$$

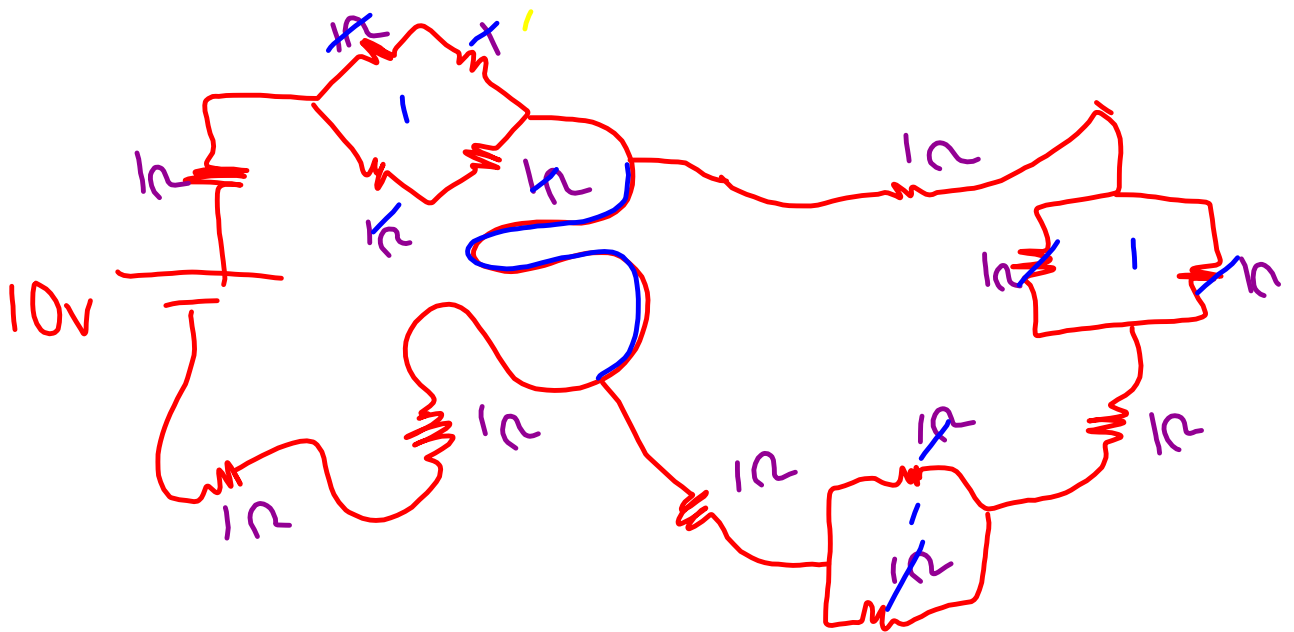
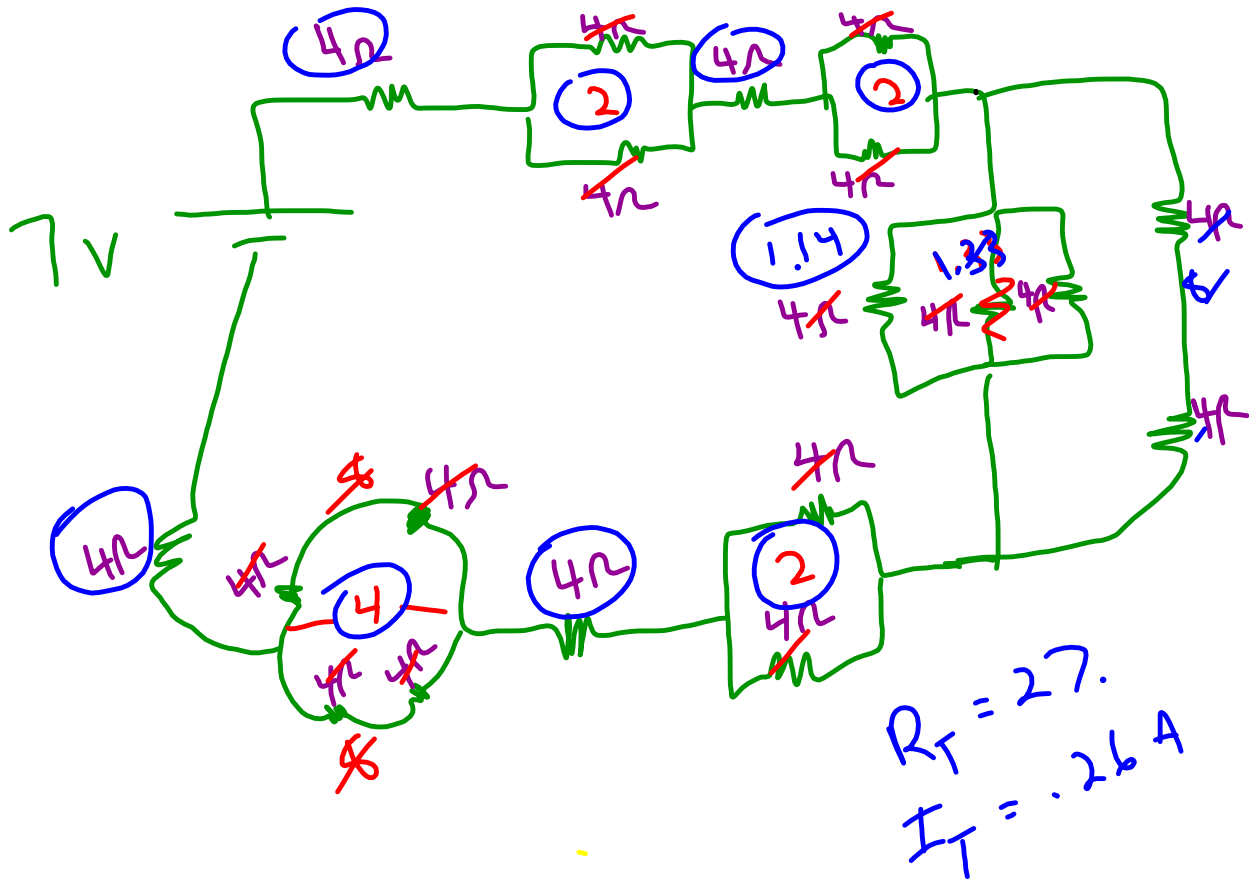
$$6 = I(22)$$

$$I_T = .27A$$



Find  $I_t$  and does the fuse blow?





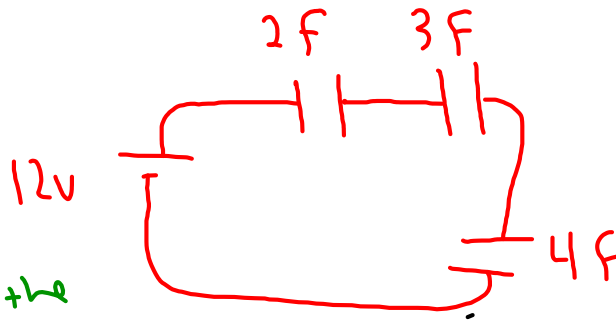
Capacitors in Circuits

$$\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2} \dots$$

Series

$$C = \frac{q}{V}$$

Charge is the same in each capacitor

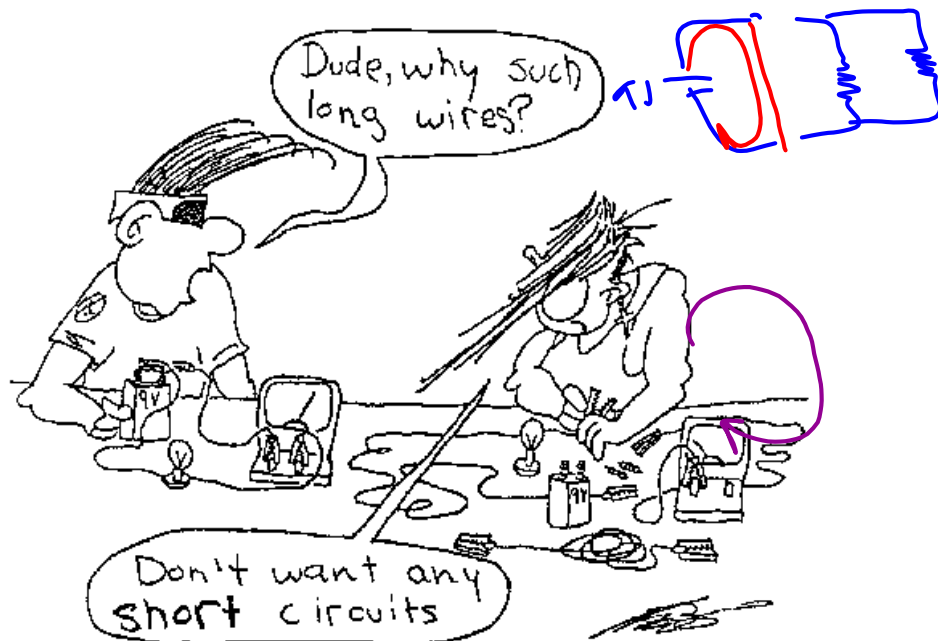


Parallel

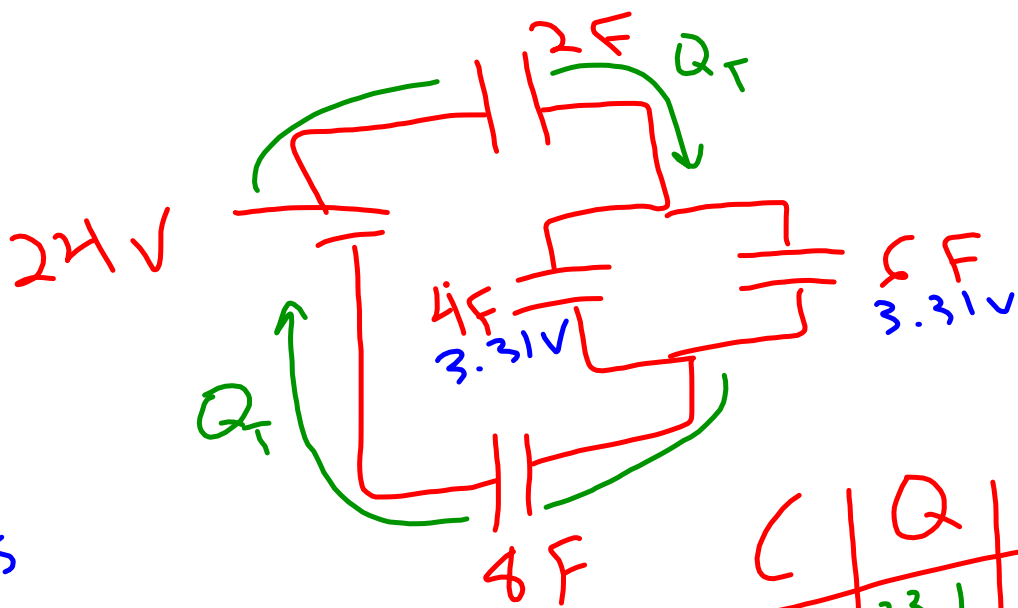


$$C_T = C_1 + C_2 \dots = F$$

Voltage stays the same across each capacitor



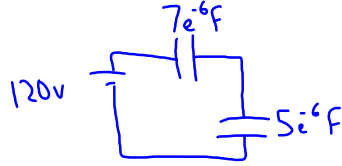
Cartoon by Ehren Stillman, a high-school student from Deroche, BC, Canada.



$$\begin{array}{r}
 24 \\
 - 16.55 \\
 - 4.14 \\
 \hline
 3.31V
 \end{array}$$

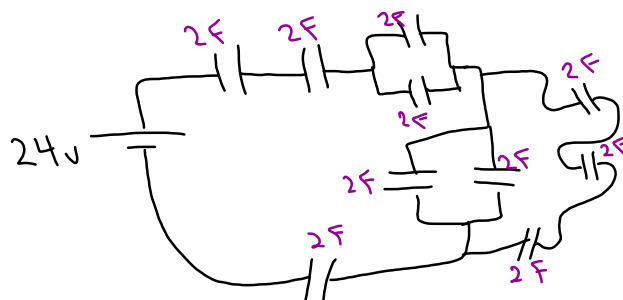
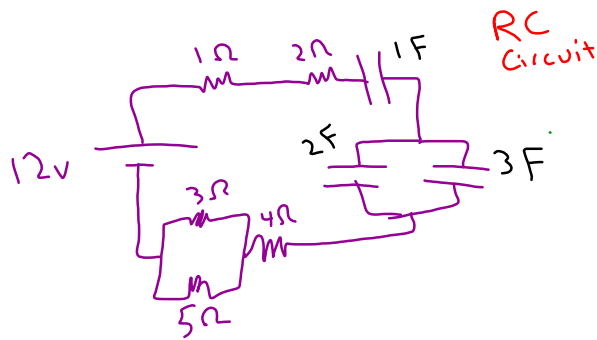
C	Q	V
2	33.1	16.55
4	13.24	3.31
6	19.46	3.31
8	33.1	4.14

Using Capacitors in circuits

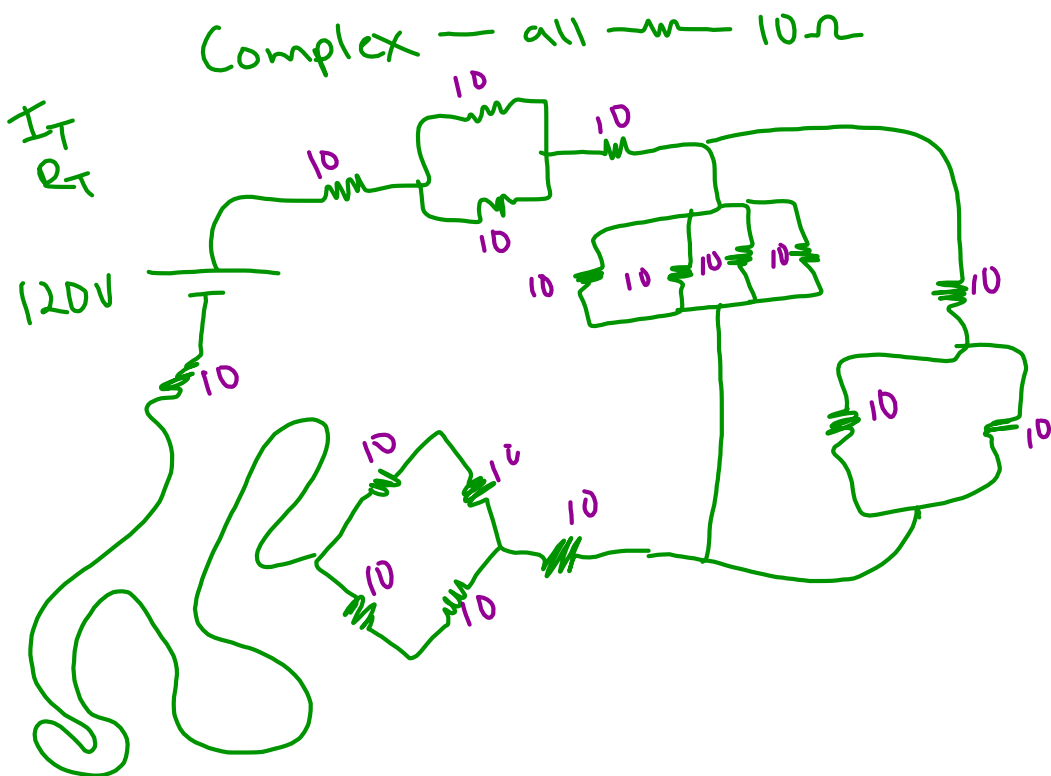
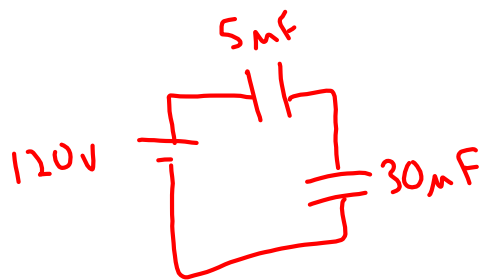
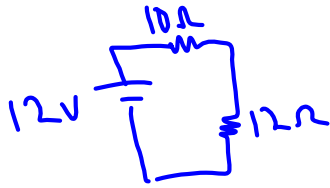


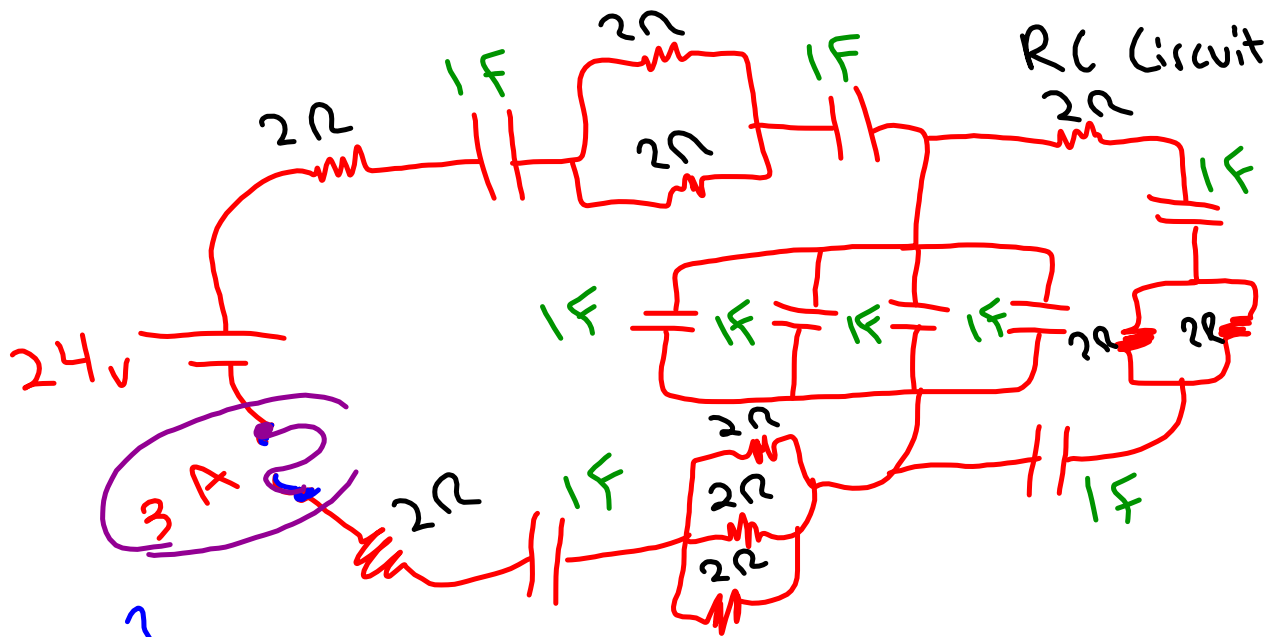
Series  
 $q$  is constant

Parallel  $\rightarrow$  Voltage is constant









$R_T = ?$   
 $I_T = ?$   
 $C_T = ?$   
 $Q_T = ?$

$I = \frac{dq}{dt}$     $C = \frac{q_0}{V_0}$     $q_0 = \text{initial}$   
 RC Circuits- when circuits contain both resistors and capacitors  
 + → amount of time passed  
 → Time Constant

Charging Capacitor  $q = q_0(1 - e^{-t/(RC)})$

$\tau = RC$

Discharging Capacitor  $q = q_0 e^{-t/(RC)}$

$\frac{q}{q_0} = e^{-t/RC}$

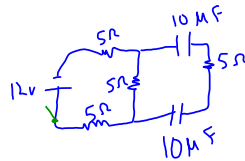
$\tau = RC$

→ time constant

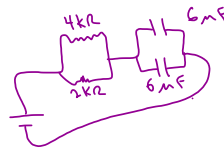
Tau is the time constant, measured in seconds because an Ohm x Farad = second. The time constant is the amount of time required for the capacitor to accumulate 63.2% of its equilibrium charge. If Tau is small it approaches its charge quickly, if Tau is large it takes a longer time to charge.

Charging

$T = ?$   
 30%  
 $\tau = RC$

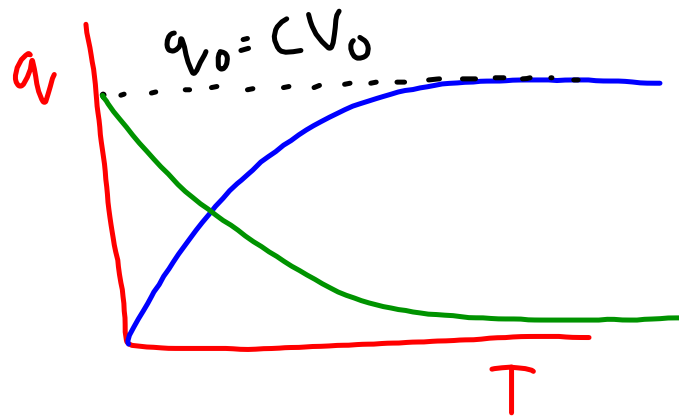


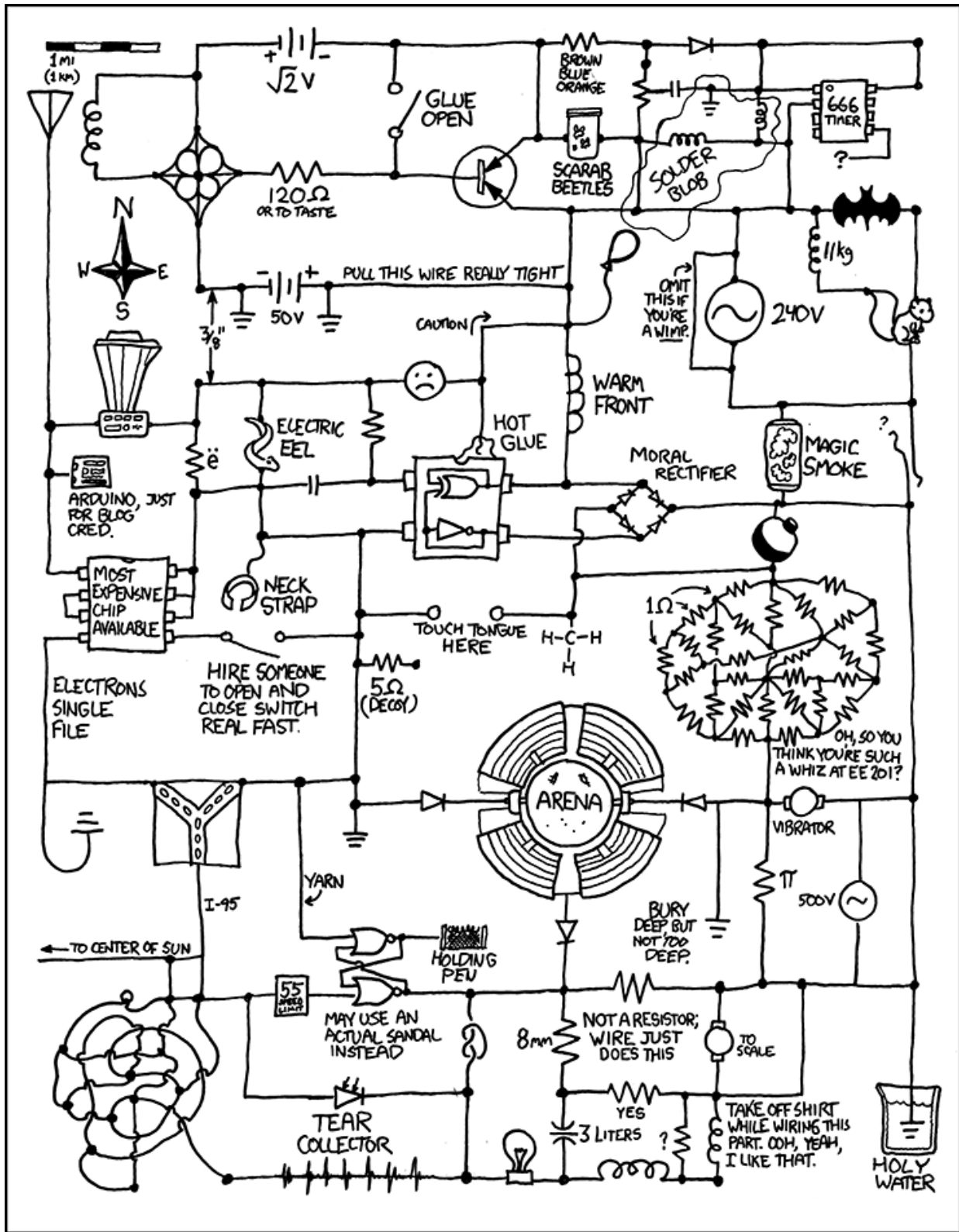
75% charged  
 $T = ?$   
 discharge



- Ch 20: 2, 5, 7, 9, 12, 13, 17, 20, 21, 24, 26, 29, 41, 44, 47, 50, 54, 58, 61, 63, 70, 73, 77, 78, 82, 86, 88, 92, 96

Green Book  
 Ch 22 MC: 22, 24, 27





**Internal Resistance-** the internal resistance of a battery will reduce the amount of voltage running through the circuit. The amount of current will also affect the voltage drop across the battery.

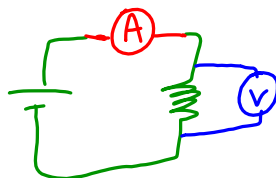
$\mathcal{E} = 12\text{V}$   
 $R_i = .01\Omega$   
 $I = 10\text{A}, 100\text{A}$   
 $V_T = ?$

$V = IR$  (inside battery)  
 $V_T = \mathcal{E} - V_i$  (perfect work leaves battery)  
 $\mathcal{E} = 12\text{V}$

$R = \frac{\rho L}{A}$  (ρ - resistivity)

$R_i = .01\Omega$   
 $V_i = .002\text{V}$   
 $V_T = 6 - .002$

- Ammeter → I → series
- Voltmeter → V → parallel
- Ohm meter → R → parallel with an open circuit



Ohmic  $\rightarrow$  resistance is constant  
regardless of current

Non ohmic  $\rightarrow$  resistance changes  
based on current

eg 724

ex. semiconductor  
diode

# Kirchoffs Law

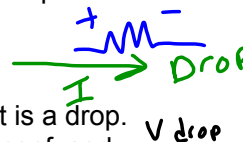
Read pg 741

Rule 1: The sum of magnitudes of the currents directed into a junction equals the sum of the magnitude of the currents directed out of a junction



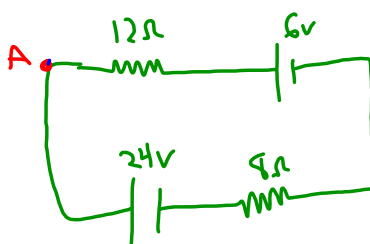
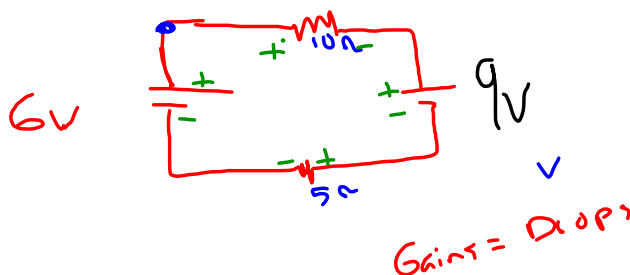
Rule 2: Around any closed-circuit loop, the sum of the potential drops equals the sum of the potential rises.

going across a battery from - to + is a potential rise  
 going across a resistor in the direction of the current is a drop.  
 Label each resistor with a plus and minus to not be confused.

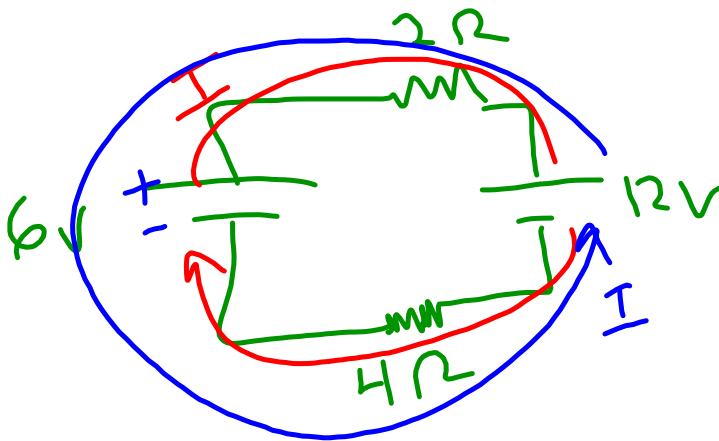


Set up a system of equations based off of each loop.

Voltage drops = Voltage Gains

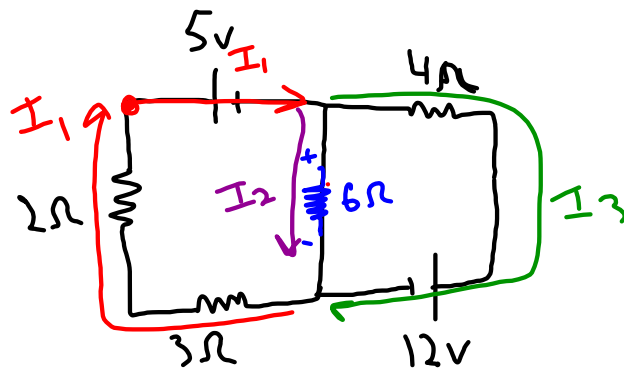






V	I	R
		2
		4





$$\begin{aligned} (-5 = 11I_2 + 5I_3) & \quad 9 \\ (-17 = 5I_2 + 9I_3) & \quad -5 \end{aligned}$$

$$\begin{aligned} -45 &= 99I_2 + 45I_3 \\ + 85 &= -25I_2 - 45I_3 \end{aligned}$$


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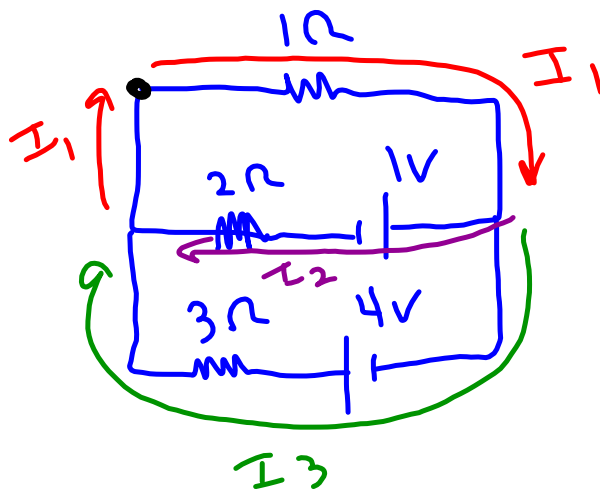

$$40 = 74I_2 \quad I_2 = .541A$$

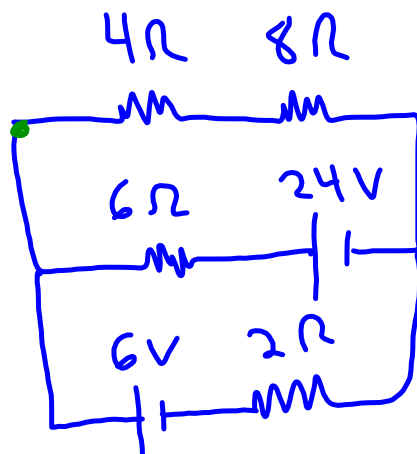
$$-5 = 6(.541) + 5I_1$$

$$I_1 = -1.65A$$

$$-1.65 = .541 + I_3$$

$$I_3 = -2.19A$$





$$I_1 = .78 A$$

$$I_2 = 2.45 A$$

$$I_3 = -1.66 A$$

$$6 = 2I_3 + 12I_1$$

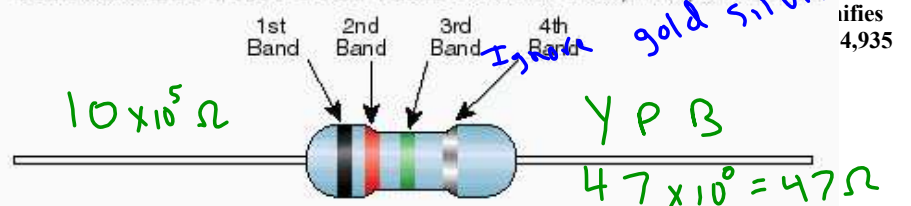
It is sometimes not obvious whether a color coded component is a resistor, capacitor, or inductor, and this may be deduced by knowledge of its circuit function, physical shape or by measurement.

A diagram of a resistor, with four color bands A, B, C, D from left to right A diagram of a 2.7 MΩ color-coded resistor.

To distinguish left from right there is a gap between the C and D bands.

- \* band A is first significant figure of component value (left side)
- \* band B is the second significant figure
- \* band C is the decimal multiplier
- \* band D if present, indicates tolerance of value in percent (no color means 20%)

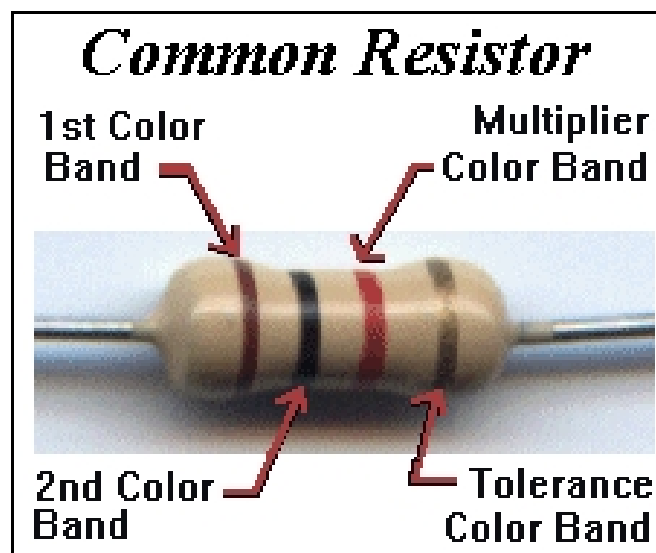
**Standard EIA Color Code Table** 4 Band: ±2%, ±5%, and ±10% (yellow



Color	1st Band (1st figure)	2nd Band (2nd figure)	3rd Band (multiplier)	4th Band (tolerance)
Black	0	0	10 <sup>0</sup>	
Brown	1	1	10 <sup>1</sup>	
Red	2	2	10 <sup>2</sup>	±2%
Orange	3	3	10 <sup>3</sup>	
Yellow	4	4	10 <sup>4</sup>	
Green	5	5	10 <sup>5</sup>	
Blue	6	6	10 <sup>6</sup>	
Violet	7	7	10 <sup>7</sup>	
Gray	8	8	10 <sup>8</sup>	
White	9	9	10 <sup>9</sup>	
Gold			10 <sup>-1</sup>	±5%
Silver			10 <sup>-2</sup>	±10%

0.2 x 10<sup>5</sup>

A resistor which (read left to right) displays the colors yellow, violet, yellow, brown. The first two bands represent the digits '4, 7'. The third band, another yellow, gives the multiplier 10<sup>4</sup>. The value is then 47 x 10<sup>4</sup> Ω, or 470 kΩ. The brown band is a then a tolerance of ±1%.



A Ohmmeter measures *resistance*  
attached to the object when circuit is  
off.

A Voltmeter measures *voltage*  
attached in parallel to the resistor when  
circuit is on

An Ammeter measures *current*  
attached in series before the resistor  
when circuit is on



## Attachments

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edison

electric man

doorknob current

xkcd Circuit Diagram.mht